

Principles of Calculus Modeling: An Interactive Approach by Donald Kreider, Dwight Lahr, and Susan Diesel
Exercises for Section 2.9

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1. (1 pt)

Find the derivative of the trigonometric function $y = \cos(7\sqrt{x})$.

$$y' = \underline{\hspace{2cm}}$$

2. (1 pt)

Find the derivative of $y = \cos(2\sin x)$.

$$y' = \underline{\hspace{2cm}}$$

3. (1 pt)

Find the derivative of $y = 8\csc\left(\frac{10}{x}\right)$.

$$y' = \underline{\hspace{2cm}}$$

A. $-8\csc\left(\frac{10}{x}\right)\cot\left(\frac{10}{x}\right)$

B. $\frac{80}{x^2}\csc\left(\frac{10}{x}\right)\cot\left(\frac{10}{x}\right)$

C. $\frac{80}{x^2}\csc x \cot x$

D. $-8\csc\left(\frac{80}{x^2}\right)\cot\left(\frac{80}{x^2}\right)$

E. None of these.

4. (1 pt)

Find the derivative of $y = \tan(-7x)\cot(-7x)$. Simplify your answer **completely**. Use either $\frac{1}{\tan x}$ or $\frac{\cos x}{\sin x}$ to express $\cot x$ and

$\frac{1}{\sin x}$ to express $\csc x$.

$$y' = \underline{\hspace{2cm}}$$

5. (1 pt)

What is the derivative of $f(t) = 10t \cos t - 10 \sin t$?

$$f'(t) = \underline{\hspace{2cm}}$$

6. (1 pt)

Find the derivative of $g(t) = \sqrt{\frac{3\cos t}{t}}$.

$$g'(t) = \underline{\hspace{2cm}}$$

7. (1 pt)

Find the derivative of $f(t) = \cos(\tan(\sin t))$.

$$f'(t) = \underline{\hspace{2cm}}$$

8. (1 pt)

Find equations for lines that are tangent and normal to the curve

$y = \cos\left(7x + \frac{\pi}{2}\right)$ at the point $(0,0)$.

Line tangent to curve:

$$y = \underline{\hspace{2cm}}$$

Line normal to curve:

$$y = \underline{\hspace{2cm}}$$

9. (1 pt)

Let $y = \sin(2x^2)$. Find each of the following.

$$y' = \underline{\hspace{2cm}}$$

$$y'' = \underline{\hspace{2cm}}$$

$$y''' = \underline{\hspace{2cm}}$$

10. (1 pt)

Let $y = \tan(-9x)$. Find each of the following.

$$y' = \underline{\hspace{2cm}}$$

$$y'' = \underline{\hspace{2cm}}$$

Express y'' in terms of y .

$$y'' = \underline{\hspace{2cm}}$$

11. (1 pt)

Let $f(x) = \sec(x)$ and $g(x) = f'(x)$. What is $g'(x)$?

$$g'(x) = \underline{\hspace{2cm}}$$

12. (1 pt)

Sisyphus, the great ruler of Corinth known for his trickery and deceit, was captured and punished in Tartalus. When captured, his punishment was to roll a heavy stone to the top of a hill. Upon reaching the top, the stone would invariably slip down the other side, forcing Sisyphus to begin anew. If the height of the stone at time t can be described by the function $f(t) = 19(\sin(t))^2$ cubits, what function describes the rate of change in the height of the stone?

$\underline{\hspace{2cm}}$ cubits / second

13. (1 pt)

Find the derivative of $19\cos(\cos(6x))$ at $x = \frac{\pi}{2}$.

$$\underline{\hspace{2cm}}$$

14. (1 pt)

Find the derivative of $\sqrt{\cos^2(5x) + \sin^2(5x)}$.

$$\underline{\hspace{2cm}}$$