

Principles of Calculus Modeling: An Interactive Approach by Donald Kreider, Dwight Lahr, and Susan Diesel  
Exercises for Section 2.11

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1. (1 pt)

Let  $3x^3 = y^2$ . Find  $y'$  in terms of  $x$  and  $y$ .

What are the slopes of the lines tangent to this curve at points where  $x = 0.6$ ? Enter answers from smallest to largest.

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2. (1 pt)

Let  $(x - 1)^4 = (y + 13)^5$ . Find  $y'$  in terms of  $x$  and  $y$ .

What are the slopes of the lines tangent to this curve at points where  $y = -13$ ? Enter answers from smallest to largest.

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3. (1 pt)

Let  $x^5y^2 = 2x + 4y$ . Find  $\frac{dy}{dx}$  in terms of  $x$  and  $y$ .

$\frac{dy}{dx} =$  \_\_\_\_\_

4. (1 pt)

Find the equation of the tangent line to the curve  $\frac{x}{y} + \left(\frac{y}{x}\right)^5 = 2$  at the point  $(-1, -1)$ . Write the equation of the line in slope-intercept form.

$y =$  \_\_\_\_\_

5. (1 pt)

Find the equation of the tangent line to the curve  $\tan(xy^2) = \frac{18xy}{\pi}$  at the point  $\left(\frac{\pi}{81}, \frac{9}{2}\right)$ . Write the equation of the line in slope-intercept form.

$y =$  \_\_\_\_\_

6. (1 pt)

Let  $14xy = 2x + 7y$ . Find  $y''$  in terms of  $x$ .

$y'' =$  \_\_\_\_\_

7. (1 pt)

Let  $s^7 + t^7 = 1$ . Find  $\frac{ds}{dt}$  in terms of  $s$  and  $t$ .

$\frac{ds}{dt} =$  \_\_\_\_\_

8. (1 pt)

For the function  $x = \sin y + \cos y$ , calculate both  $\frac{dy}{dx}$  and  $\frac{dx}{dy}$ .

Write your answers in terms of sine and cosine.

$\frac{dy}{dx} =$  \_\_\_\_\_

$\frac{dx}{dy} =$  \_\_\_\_\_

9. (1 pt)

For the function  $x^3y^7 + 16xy^9 = 0$ , calculate both  $\frac{dy}{dx}$  and  $\frac{dx}{dy}$ .

$\frac{dy}{dx} =$  \_\_\_\_\_

$\frac{dx}{dy} =$  \_\_\_\_\_

10. (1 pt)

For the function  $\cos x \sin y + x^5 = 11$ , calculate both  $\frac{dy}{dx}$  and  $\frac{dx}{dy}$ .

Write your answers in terms of sine and cosine.

$\frac{dy}{dx} =$  \_\_\_\_\_

$\frac{dx}{dy} =$  \_\_\_\_\_