

218. **Coroll. 2.** Ducto arcu  $MR$ , quia ad utrumque quadrantem est normalis, triangulum sphaericum  $\triangleq MN$ , in quo dantur latera  $\triangleq M = \sigma$ ,  $\triangleq N = \vartheta - \psi$  et angulus  $M \triangleq N$  inventoque latere  $MN$  cum angulo  $\triangleq MN$ , erit  $\lambda = MN$  et  $\sin \mu = \sin \lambda \cos \triangleq MN$ .

219. **Coroll. 3.** Loco tempusculi  $dt$  spatium non solum aliquot horarum sed etiam dierum capi potest, nisi positio corporis  $N$  ratione ipsius  $M$  citissime varietur. Tum ex motu malo pro hoc temporis spatio colligatur angulus  $d\zeta$ , indeque erit  $edq = cd\zeta \sqrt{cp}$ , quem valorem in singulis perturbationibus momentaneis substitui oportet.

220. **Scholion.** Ex his principiis perturbationes motus cujusque planetae principalis defini poterunt, quatenus ab actione alius planetae vel etiam cometae oriuntur; ad planetas autem secundarios, seu satellites, haec methodus minus commode accommodari potest, quandoquidem assumimus remoto corpore perturbante, motum futurum esse regularem; hinc itaque perturbationes lunae, quae forte ab actione cujusdam planetae vel cometae proficiscuntur, determinare nequeant. Sin autem ipse sol ut corpus perturbans consideretur, sine cujus actione luna motum regularem esset habitura, inaequalitates motus lunae hinc concludere licebit, sed quia actio solis est perennis collectio perturbationum momentanearum conclusionem nimis lubricam reddit. Maximum autem usum haec methodus praestabit, si actio cujuspiam cometae in motum planetae principalis, per viciniam cometa transit, investigari debeat: quoniam enim actio cometae non diutius manet sensibilis quam dum ejus distantia a planeta fuerit, valde parva, omnino superfluum foret, totam actionem quam cometa per totum suum tempus periodicum exerit, exquirere velle, quem in finem integram nostrarum formularum exhiberi (opus esset). Sufficiet igitur per breve tempus effectum cometae in orbita cujuspiam planetae perturbanda cognovisse, id quod ope formularum differentialium haud difficulter praestabitur. Casus autem, quibus cometae ad planetas tam prope accedunt, ut perturbationem notabilem efficere queant, vehementer raro accidunt. Ac si cometa anni 1682 secundum praedictionem Cel. Clairaut hoc anno 1759 revertatur, phaenomena imprimis singularia in motu terrae ab ejus actione expectari possent, propterea quod in satis exigua a terra distantia praeterebatur. Opera ergo pretium erit, ope formularum traditarum in perturbationem motus terrae quae orbitae, ab actione hujus cometae oriundam, inquirere; ut deinceps, quando elementa motus istius cometae accuratius erunt definita, ad hoc exemplum plenior investigatio suscipi possit.

### Digressio

qua effectus Cometae A. 1759 expectati in motu terrae perturbando investigatur.

V. II. Primo quidem assumo hunc cometam secundum eadem elementa latum iri, quae per apparitionem A. 1682 sunt determinata. Etsi enim ob actionem Jovis et Saturni, ejus tempus periodicum quasi biennio fuit retardatum, ob eandemque rationem ejus reliqua motus elementa haud mutationes subisse probabile, tamen quia de eorum valore praesente nihil certi constat, dante

cometae denuo definire licuerit, elementis superioris revolutionis utar. Posita ergo distantia a sole = 100000, statuum pro hoc cometa

1. Distantiam perihelii a sole = 58328
2. Semiparametrum = 116656
3. Nodum ascendentem 1° 21' 16"
- Nodum descendentem 7° 21' 16"
4. Distantiam nodi desc. a perih. 71° 36'
5. Inclinationem ad eclipticam 17° 56'
6. Longitudinem perihelii 10° 2' 52".

Motus autem hujus cometae est retrogradus, et a nodo ascendente ad perihelium, indeque ad nodum descendentem pergit.

Qui hunc cometam primum mense Januario hujus anni 1759 viderant, suspicantur eum die 14 Martii per perihelium suum transiisse, ex quo postquam per nodum descendentem fuerit processisset ad terram proxime accedet. Nodum descendentem autem attinget circa d. 14 Aprilis, unde post hoc tempus loca cometae colligi conveniet. At ex mea theoria motus cometarum elapsis diebus post transitum per perihelium habetur  $l(t + \frac{1}{3}t^3) = l\delta + 8,4362521$ , unde anomalia vera angulus a perihelio confectus definitur, quae si vocetur =  $\zeta$ , erit distantia ejus a sole =  $\frac{58328}{\cos^2 \frac{1}{2}\zeta}$

III. Posito ergo cometam ipso meridie die 14 Martii per perihelium transiisse, die 14 Aprilis sequentibus loca cometae ita se habebunt:

Diebus a perihelio	A. 1759	Anomalia vera	ejus semissis	distantia a sole	distantia a nodo descend.
31	April 14 <sup>a</sup>	71° 37'	35° 49'	88705	0° 1'
32	15	72 56	36 28	90187	1 20
33	16	74 13	37 7	91731	2 37
34	17	75 28	37 44	93254	3 52
35	18	76 41	38 21	94838	5 15
36	19	77 51	38 55	96349	6 15
37	20	78 58	39 29	97916	7 22
38	21	80 3	40 2	99493	8 29
39	22	81 17	40 34	101070	9 31
40	23	82 8	41 4	102641	10 32
41	24	83 8	41 34	104200	11 32
42	25	84 16	42 3	105782	12 30
43	26	85 2	42 31	107360	13 26
44	27	85 57	42 58	108931	14 21
45	28	86 50	43 25	110550	15 14
46	29	87 42	43 51	112133	16 6
47	30	88 32	44 16	113745	16 56
48	Maji 1	89 21	44 41	115380	17 45
49	2	90 8	45 4	116925	18 32
50	3	90 54	45 27	118517	19 18
51	4	91 39	45 50	120150	20 3
52	5	92 23	46 12	121754	20 47
53	6	93 5	46 34	123401	21 29

IV. Nunc quoque ad singulos hos dies local terrae ex sole visa ex tabulis colligamus, simul distantias ejus a nodo descendente orbitae cometae, qui cadit in  $7^{\circ} 21' 16''$  notemus. Prohodie tempore erat locus perihelii terrae in  $3^{\circ} 8' 39''$ , ejus ergo distantia a nodo descendente est  $= 4^{\circ} 12' 77''$ .

A. 1789	Distantia terrae a sole	Longitudo terrae	Dist. terrae a nodo desc.
Aprilis 14 <sup>d</sup>	100400	6° 23' 13'	0° 28' 3"
15	100420	6 24 11	27 5
16	100450	25 10	26 6
17	100480	26 9	25 7
18	100510	27 7	24 9
19	100540	28 6	23 10
20	100565	29 4	22 12
21	100590	7 0 3	21 13
22	100620	1 1	20 15
23	100650	1 59	19 17
24	100675	2 58	18 18
25	100700	3 56	17 20
26	100725	4 55	16 21
27	100750	5 53	15 23
28	100775	6 51	14 25
29	100800	7 49	13 27
30	100825	8 47	12 29
Maji 1	100850	9 45	11 31
2	100875	10 43	10 33
3	100900	11 41	9 35
4	100925	12 40	8 36
5	100950	13 38	7 38
6	100975	14 36	6 40

V. Pro orbita terrae porro sumitur semiaxis transversus = 100000 et excentricitas = 0,0169 unde fit semiparameter = 97144. His elementis constitutis patet circa dies 27 et 28 Aprilis cometam terrae fore proximum. Investigemus ergo perturbationes ab actione cometae oriundas in motu terrae ab 25 Aprilis usque ad 30 ejusdem, et constituamus quina intervalla spatio 24 horarum aequalia, ita tempus  $dt$  unum diem, et ex motu terrae medio  $d\zeta$  angulum  $59' 8''$  denotet, unde elementum  $d\varphi$  definiri debet. Cum autem terra continuo propius ad nodum descendente progrediatur, dum cometa ab eo recedit, angulus  $d\varphi$  negative capiendus est.

VI. Repraesentet ergo (Fig. 190) tabula planum orbitae cometae, in quo sit  $L$  sol,  $A$  perihelium cometae, a quo per arcum parabolicum  $AN$  progrediatur.  $BM\Omega$  vero sit orbita terrae a perihelio  $B$  per  $M$  ad nodum  $\Omega$  progredientis, cujus motus respectu cometae ut retrogradus spectari debet, et portio  $BM\Omega$  supra orbitam cometae versabitur. Erit ergo angulus  $BL\Omega = 132^{\circ} 27'$  et inclinatio orbitae cometae ad orbitam terrae  $\omega = 17^{\circ} 56'$ . Quodsi nunc terra haereat in  $M$ , cometa vero in  $N$ , erit  $LM = r$ ,  $LN = u$ ,  $MN = w$ ,  $BLM = -s$ ,  $ALN = \vartheta$ ,  $AL\Omega = \psi = 71^{\circ} 36'$  et  $\Omega LN = \vartheta - \psi$ ; porro  $\Omega LM = \sigma$ , atque  $r = 100000$ ,  $p = 97144$  et  $q = 0,0169$ . Denique positis massis solis, terrae et cometae  $L, M, N$ , sit  $\frac{N}{L+M} = n$ , unde calculi perturbationum pro singulis intervallis diurnis habebunt:

Calculus pro intervallo a 25 ad 26 Aprilis.

Cum sit  $p = 97144$ ,  $q = 0,0169$ ,  $r = 100000$  et  $\omega = 17^\circ 56'$ , erit  $v = 100700$ ,  $u = 105782$ ,  
 $LM = \sigma = 17^\circ 20'$ ,  $s = -115^\circ 17'$ ,  $\vartheta - \psi = 12^\circ 30'$ . Nunc ob  $c = 100000$ , ob  $d\varphi = \frac{-cd\xi\sqrt{cp}}{v}$   
 erit  $d\xi = 3548''$  colligitur

$lcp = 9,9874160$	$lc\sqrt{cp} = 9,9937080$
$l\sqrt{cp} = 4,9937080$	$ld\xi = 3,5499836$
$lc = 5,0000000$	<u>13,5436916</u>
$lc\sqrt{cp} = 9,9937080$	$lv = 10,0060590$
$lv = 5,0030295$	$l - d\varphi = 3,5376326$
	<u>4,6855749</u>
	$l - d\varphi = 8,2232075$

Erit ergo pro terminis, ubi  $d\varphi$  angulum denotat,  $d\varphi = -3449''$ , at pro terminis, ubi in partibus  
 radii exprimi debet,  $d\varphi = -0,016719$ . Pro angulis autem  $\lambda$  et  $\mu$  calculus ita se habebit:

$l \cos(\vartheta - \psi) = 9,9895815$	$l \sin(\vartheta - \psi) = 9,3353368$
$l \cos \sigma = 9,9798158$	$l \cos \omega = 9,9783702$
$l \sin \sigma = 9,4741146$	$l \cos \omega \sin(\vartheta - \psi) = 9,3137070$
<u>9,9693973</u>	$l \sin \sigma = 9,4741146$
<u>9,4636961</u>	$l \cos \sigma = 9,9798158$
	<u>8,7878216</u>
	<u>9,2935228</u>
$+ 0,93196$	$+ 0,29087$
$+ 0,06135$	<u><math>- 0,19657</math></u>
$\cos \lambda = + 0,99331$	$\sin \mu = 0,09430$
$\lambda = 6^\circ, 38'$	$\mu = 5^\circ, 25'$

Hinc pro distantia  $LN = \varphi = \frac{v \sin \lambda}{\sin \nu}$  existente  $\text{tang } \nu = \frac{v \sin \lambda}{u - v \cos \lambda}$

$lv = 5,0030295$	$u = 105782$
$l \sin \lambda = 9,0626386$	$v \cos \lambda = 100026$
$l \cos \lambda = 9,9970829$	<u><math>u - v \cos \lambda = 5756</math></u>
$lv \sin \lambda = 4,0656681$	$lv \sin \lambda = 4,0656681$
$lv \cos \lambda = 5,0001124$	$l(u - v \cos \lambda) = 3,7601208$
<u><math>l \sin \nu = 9,9524188</math></u>	$l \text{ tang } \nu = 10,3055473$
$lv = 4,1132493$	$\nu = 63^\circ, 40'$
$lc = 5,0000000$	$\omega = 12979$
$l \frac{c^2}{w^2} = 0,8867507$	$lu = 5,0244118$
$l \frac{c^3}{w^3} = 2,6602521$	$l \frac{c^2}{w^2} = 9,9755882$
$l \frac{c^3}{w^3} = 457,354$	$l \frac{c^3}{w^3} = 9,9267646$
	$\frac{c^3}{w^3} = 0,84482$

ergo  $\frac{c^3}{w^3} - \frac{c^3}{u^3} = 456,509$  et  $lc^3 \left( \frac{1}{w^3} - \frac{1}{u^3} \right) = 2,6594494.$

Cum nunc sit

$$dp = -\frac{2nw^3}{c^3} d\varphi \sin \mu \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right)$$

reperietur variatio semiparametri  $p$ ;

$$\begin{aligned} l \frac{v^3}{c^3} &= 0,0090885 \\ lu &= 5,0244118 \\ l \sin \mu &= 8,9749624 \\ l \cdot \lambda &= 2,6594494 \\ l - d\varphi &= 8,2232075 \end{aligned}$$

erit ergo

$$\begin{aligned} dp &= 2n \cdot 77825 \\ \text{seu } dp &= 155650 n. \end{aligned}$$

$$4,8911196$$

Unde si massa cometæ aequalis esset massæ terræ, foret  $n = \frac{1}{227000}$ , ideoque proxime  $dp = \frac{1}{227000}$  autem cometa massam haberet Jovi æqualem, foret  $n = \frac{1}{1033}$ , ideoque  $dp = 151$ , qui effectus in vallo unius diei productus satis esset notabilis, cum sit  $p = 97144$ , ideoque abiret in 97295, parte  $\frac{1}{643}$  augetur.

Pro variatione semiaxis transversi  $r = 100000$  habemus hanc formulam:

$$dr = -\frac{2nqr}{p} \cdot \frac{v^3}{c^3} \cdot \frac{c^3}{w^3} \cdot d\varphi \sin s - \frac{2nr\tau v}{c^3} d\varphi \left( \sin \mu - \frac{qv}{p} \cos \lambda \sin s \right) \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right)$$

cujus formulæ calculus ita se habet:

$$lqr^2 = 8,2278867$$

$$lp = 4,9874160$$

$$3,2404707$$

$$l \frac{v^3}{c^3} = 0,0090885$$

$$l \frac{c^3}{w^3} = 2,6602521$$

$$l - d\varphi = 8,2232075$$

$$l - \sin s = 9,9562678$$

$$4,0892866$$

pars I = - 2n. 12283

pars II = + 2n. 89456

$$dr = + 2n. 77173$$

$$dr = + 154346n$$

$$\sin \mu = 0,09430$$

$$l \frac{q}{p} = 3,2404707$$

$$lv = 5,0030295$$

$$l \cos \lambda = 9,9970829$$

$$l - \sin s = 9,9562678$$

$$8,1968509$$

$$-\frac{qv}{p} \cos \lambda \sin s = + 0,01573$$

$$0,11093$$

$$l \dots = 9,0415111$$

$$lu = 5,0244118$$

$$l \frac{v}{c} = 0,0030295$$

$$l - d\varphi = 8,2232075$$

$$l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = 2,6594494$$

$$4,9516093.$$

Semixis ergo transversus fere par augmentum accipit atque semiparameter, atque hac actione tempus periodicum augetur in ratione 1 ad 1 + 2,31519n, seu annus augmentum capiet

$$= 845n \text{ dierum} = 18280n \text{ hor.} = 1096800n \text{ min.}$$

unde si cometa terrae esset aequalis, augmentum anni hinc natum foret = 4', 50".

Pro excentricitate q, cum sit  $p = (1 - qq)r$ , erit

$$qq = 1 - \frac{p}{r} \quad \text{et} \quad 2q dq = \frac{-r dp + p dr}{rr} = -\frac{dp}{r} + \frac{p dr}{rr}$$

ergo hic calculus	$lp = 5,1921491$	$lp = 4,9874160$
	$lqr = 3,2278867$	$ldr = 5,1884954$
	<u>1,9642624</u>	<u>10,1759114</u>
	- 92,100n	$lqn = 8,2278867$
		<u>1,9480247</u>
		+ 88,720n

ergo  $dq = -46,05n + 44,36n = -1,69n$ ,

unde patet excentricitatem fere nullam pati mutationem, nisi massa cometae plurimum superet massam terrae; si sit aequalis massae Jovis, fiet  $dq = -0,00164$  et  $q + dq = 0,01426$ , unde equatio centri valde imminueretur.

Pro variatione perihelii in orbita, si ponamus angulum  $\Omega LB = \alpha$ , formula supra inventa ita approximatur:

$$d\alpha = \frac{nv^3 d\varphi}{qc^3} \left( \frac{c^3 \cos s}{w^3} - \frac{u}{p} \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) \left( (1 + q \cos s) \cos \lambda \cos s + (2 + q \cos s) \sin \mu \sin s \right) \right),$$

quae ergo ita evolvetur ob  $1 + q \cos s = \frac{p}{r}$ :

$lp = 4,9874160$	$2 + q \cos s = 1,96469$
$lv = 5,0030295$	$l(2 + q \cos s) = 0,2933161$
$l(1 + q \cos s) = 9,9843865$	$l \sin \mu = 8,9749624$
$l \cos \lambda = 9,9970829$	$l \sin s = -9,9562678$
$l \cos s = -9,6305243$	<u>-9,2245463</u>
<u>-9,6119937</u>	

pars postrema = - 0,40925 - 0,16770 = - 0,57695

$l \text{ partis postr.} = -9,7611382$	$l \frac{c^3}{w^3} = 2,6602521$
$l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = +2,6594494$	$l \cos s = -9,6305243$
$lu = 5,0244118$	<u>-2,2907764</u>
<u>-7,4449994</u>	$l \text{ aggr.} = 1,9612787$
$lp = 4,9874160$	$l \frac{v^3}{c^3} = 0,0090885$
<u>-2,4515834</u>	$ld\varphi = -3,5376326$

pars post. = + 286,803

pars prior = - 195,333

lucra aggreg. = + 91,470

ergo erit

$d\alpha = -19059570n \text{ min. sec.}$

Cum igitur angulus  $\alpha$  minuatur, perihelium in orbita secundum seriem signorum promovetur et quidem hoc die, si cometa terrae esset aequalis, per  $84''$ .

Porro pro variatione nodi  $\Omega$ posito angulo  $AL\Omega = \psi$ , erit

$$d\psi = -\frac{mu}{p} \cdot \frac{v^3}{c^3} \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) d\varphi \sin \sigma \sin (\vartheta - \psi)$$

et pro variatione inclinationis  $d\omega = \frac{d\psi \sin \omega}{\tan \sigma}$ ;

calculus ergo instituatur ut sequitur:

$\frac{l^u}{p} = 0,0369958$	ergo	$d\psi = + 112880 n \text{ min. sec.}$
$\frac{l^{v^3}}{c^3} = 0,0090885$		$ld\psi = 5,0526177$
$l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = 2,6594494$		$l \sin \omega = 9,4884240$
$ld\varphi = -3,5376326$		$4,5410417$
$l \sin \sigma = 9,4741146$		$l \tan \sigma = 9,4942988$
$l \sin (\vartheta - \psi) = 9,3353368$		$ld\omega = 5,0467429$
$-5,0526177$	ergo	$d\omega = + 111364 n \text{ min. sec.}$

unde linea nodorum  $L\Omega$  in orbita cometae promovetur angulo  $d\psi = 112880 n \text{ min. sec.}$  et inclinatio orbitae terrestris augetur angulo  $d\omega = 111364 n \text{ min. sec.}$ , quae mutationes circiter 170 vicibus sunt minores ea, quam linea absidum terrae experitur.

#### Calculus pro intervallo a 26 ad 27 Aprilis.

Cum sit  $p = 97144$ ;  $q = 0,0169$ ;  $r = 100000$ , et  $\omega = 17^\circ, 56'$ , erit  $v = 100725$ ;  $u = 107360$   
 $\Omega LM = \sigma = 16^\circ, 21'$ ;  $s = -116^\circ, 16'$ ;  $\vartheta - \psi = 13^\circ, 26'$ . Nunc pro  $d\varphi$  inveniend

$lv = 5,0031373$	$ld\zeta\sqrt{cp} = 13,5436916$
	$lvv = 10,0062746$
	$l - d\varphi = 3,5374170$
	$4,6855749$
	$l - d\varphi = 8,2229919$

priori valore in mutatione angulorum, posteriori longitudinum est utendum.

Nunc pro angulis  $\lambda$  et  $\mu$  inveniendis erit

$l \cos (\vartheta - \psi) = 9,9879525$	$l \sin (\vartheta - \psi) = 9,3660750$
$l \cos \sigma = 9,9820721$	$l \cos \omega = 9,9783702$
$l \sin \sigma = 9,4494849$	$9,3444452$
$9,9700246$	$l \sin \sigma = 9,4494849$
$9,4374374$	$l \cos \sigma = 9,9820721$
	$8,7939301$
	$9,3265173$

$$\begin{aligned}
 &+ 0,93331 \\
 &+ 0,06222 \\
 \cos \lambda &= 0,99553 \\
 \lambda &= 5^{\circ}, 25' \\
 \text{dista. } MN &= \omega \text{ ita invenitur} \\
 l\nu &= 5,0031373 \\
 l \sin \lambda &= 8,9749624 \\
 l \cos \lambda &= 9,9980563 \\
 l\nu \sin \lambda &= 3,9780997 \\
 l\nu \cos \lambda &= 5,0011936 \\
 l \sin \nu &= 9,9040529 \\
 l\omega &= 4,0740468 \\
 l \frac{c^2}{w} &= 0,9259532 \\
 l \frac{c^3}{w^3} &= 2,7778596 \\
 \frac{c^3}{w^3} &= 599,597
 \end{aligned}$$

$$\begin{aligned}
 &+ 0,27380 \\
 &- 0,21209 \\
 \sin \mu &= 0,06171 \\
 \mu &= 3^{\circ}, 32' \\
 u &= 107360 \\
 \nu \cos \lambda &= 100275 \\
 u - \nu \cos \lambda &= 7085 \\
 l\nu \sin \lambda &= 3,9780997 \\
 l(u - \nu \cos \lambda) &= 3,8503399 \\
 l \text{ tang } \nu &= 10,1277598 \\
 \nu &= 53^{\circ}, 18' \\
 \omega &= 11859 \\
 lu &= 5,0308425 \\
 l \frac{c}{u} &= 9,9691575 \\
 l \frac{c^3}{u^3} &= 9,9074725 \\
 \frac{c^3}{u^3} &= 0,8081.
 \end{aligned}$$

$$\frac{c^3}{w^3} - \frac{c^3}{u^3} = 598,789$$

et  $l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = 2,7772738.$

Pro variatione parametri p:

$$\begin{aligned}
 l \frac{v^3}{c^3} &= 0,0094179 \\
 lu &= 5,0308425 \\
 l \sin \mu &= 8,7897867 \\
 l \dots &= 2,7772738 \\
 l - d\varphi &= 8,2229919 \\
 &= 4,8303128
 \end{aligned}$$

erit ergo

$$\begin{aligned}
 dp &= 2n \cdot 67657 \\
 \text{seu } dp &= + 135314n \\
 &\text{minor quam die praecedente.}
 \end{aligned}$$

Pro variatione semiaxis transversis r:

$$\begin{aligned}
 l \frac{qrr}{p} &= 3,2404707 \\
 l \frac{v^3}{c^3} &= 0,0094119 \\
 l \frac{c^3}{w^3} &= 2,7778596 \\
 l - d\varphi &= 8,2229919 \\
 l - \sin s &= 9,9526685 \\
 &= 4,2034026 \\
 \text{pars I} &= - 2n \cdot 15963 \\
 \text{pars II} &= + 2n \cdot 83696 \\
 dr &= + 2n \cdot 67733 \\
 dr &= 135466n
 \end{aligned}$$

$$\begin{aligned}
 l \frac{q}{p} &= 3,2404707 \\
 l\nu &= 5,0031373 \\
 l \cos \lambda &= 9,4980563 \\
 l - \sin s &= 9,9526685 \\
 &= 8,1943328 \\
 - \frac{qv}{p} \cos \lambda \sin s &= + 0,01564 \\
 \sin \mu &= 0,06171 \\
 &= 0,07735 \\
 l \dots &= 8,8884603 \\
 lu &= 5,0308425 \\
 l \frac{v}{c} &= 0,0031373 \\
 l - d\varphi ( ) &= 1,0002657 \\
 &= 4,9227058
 \end{aligned}$$



Pro excentricitatis  $q$  variatione,

$ldp = 5,1313428$	$lp = 4,9874160$
$lqr = 3,2278867$	$ldr = 5,1318304$
$1,9034541$	$0,1192464$
$-80,067$	$lqrr = 8,2278867$
$+79,681$	$1,9013597$
$2dq = -0,386n$	$et dq = -0,193n.$

Pro variatione anguli  $\Omega LB = \alpha$ :

$lp = 4,9874160$	$2 + q \cos s = 1,96445$
$lv = 5,0031373$	$l(2 + q \cos s) = 0,2932409$
$l(1 + q \cos s) = 9,9842787$	$l \sin \mu = 8,7897867$
$l \cos \lambda = 9,9980563$	$l \sin s = -0,9526685$
$l \cos s = -9,6459619$	$-9,0356961$
$-9,6282969$	

$$\text{pars postrema} = -0,42491 - 0,10857 = -0,53348$$

$l \text{ part. postr.} = -9,7271181$	$l \frac{c^3}{w^3} = 2,7778596$
$l \left( \frac{c^3}{w^3} - \frac{c^3}{n^3} \right) = 2,7772738$	$l \cos s = -9,6459619$
$lu = 5,0398425$	$-2,4238215$
$-7,5352344$	
$lp = 4,9874160$	$l \text{ aggr.} = 1,9469433$
$-2,5478184$	$l \frac{v^3}{c^3} = 0,0094119$
	$ld\varphi = -3,5374170$
$\text{pars posterior} = +353,85$	$-5,4937722$
$\text{pars prior} = -265,35$	$lq = 8,2278867$
$\text{aggreg.} = +88,50$	$-7,2658859.$

Ergo

$$d\alpha = -18445310n \text{ min. sec.}$$

Pro variatione nodi et inclinationis:

$l \frac{u}{p} = 0,0434265$	Ergo $d\psi = +152436n \text{ min. sec.}$
$l \frac{v^3}{c^3} = 0,0094119$	$ld\psi = +5,1830891$
$l \left( \frac{c^3}{w^3} - \frac{c^3}{n^3} \right) = 2,7772738$	$l \sin \omega = 9,4884240$
$ld\varphi = -3,5374170$	$l \cos \sigma = 0,5325872$
$l \sin \sigma = 9,4494849$	$+6,2041003$
$l \sin (\vartheta - \psi) = 9,3660750$	
$-5,1830891$	ergo $d\omega = +1599927n \text{ min. sec.}$

**Calculus pro intervallo a 27 ad 28 Aprilis.**

Cum sit  $p = 97144$ ,  $q = 0,0169$ ;  $r = 100000$ , et  $\omega = 17^\circ, 56'$ , erit  $\nu = 100750$ ;  $u = 108931$ ;  
 $\sigma = 15^\circ, 23'$ ,  $s = -117^\circ, 14'$ ;  $\vartheta - \psi = 14^\circ, 21'$ .

$lv = 5,0032451$	$l \operatorname{cd} \zeta \sqrt{cp} = 13,5436916$
$lu = 5,0371515$	$lvv = 10,0064902$
$lp = 4,9874160$	$l - d\varphi = 3,5372014$
$l \frac{u}{p} = 0,0497355$	$4,6855749$
	$l - d\varphi = 8,2227763$

Hinc pro angulis  $\lambda$  et  $\mu$

$l \cos (\vartheta - \psi) = 9,9862340$	$l \sin (\vartheta - \psi) = 9,3941794$
$l \cos \sigma = 9,9841548$	$l \cos \omega = 9,9783702$
$l \sin \sigma = 9,4236974$	$9,3725496$
$9,9703888$	$l \sin \sigma = 9,4236974$
$9,4099314$	$l \cos \sigma = 9,9841548$
	$8,7962470$
	$9,3567044$
$+ 0,93409$	$+ 0,25700$
$+ 0,06255$	$- 0,22735$
$\cos \lambda = 0,99664$	$\sin \mu = 0,02965$
$\lambda = 4^\circ, 42'$	$l \sin \mu = 8,4720247,$

unde colligitur distantia  $\omega$

$lv = 5,0032451$	$u = 108931$
$l \sin \lambda = 8,9134881$	$v \cos \lambda = 100411$
$l \cos \lambda = 9,9985372$	$u - v \cos \lambda = 8520$
$lv \sin \lambda = 3,9167332$	$lv \sin \lambda = 3,9167332$
$lv \cos \lambda = 5,0017823$	$l (u - v \cos \lambda) = 3,9304396$
$l \sin \nu = 9,8425548$	$l \operatorname{tang} \nu = 9,9862936$
$lvv = 4,0741784$	$\nu = 44^\circ, 6'$
$l \frac{v}{w} = 0,9258216$	$l \frac{v}{u} = 9,9628485$
$l \frac{v^3}{w^3} = 2,7774648$	$l \frac{v^3}{u^3} = 9,8885455$
$l \frac{v^3}{w^3} = 599,05$	$\frac{v^3}{u^3} = 0,7706$
	$\frac{v^3}{w^3} - \frac{v^3}{u^3} = 598,27$
	$l \left( \frac{v^3}{w^3} - \frac{v^3}{u^3} \right) = 2,7768972$

Pro variatione parametri  $p$ :

$$\begin{aligned} l \frac{p^3}{e^3} &= 0,0097353 \\ lu &= 5,0371515 \\ l \sin \mu &= 8,4720247 \\ l \dots &= 2,7768972 \\ l - d\varphi &= -8,2227763 \\ &+ 4,5185851 \end{aligned}$$

$$\begin{aligned} \text{Ergo} \\ dp &= 2n \cdot 33005 \\ \text{seu } dp &= +66010n \\ ldp &= 4,8196097 + lu \end{aligned}$$

Pro variatione semiaxis transversi  $r$ :

$$\begin{aligned} l \frac{r^2}{p} &= 3,2404707 \\ l (e^3 : e^3) &= 0,0097353 \\ l (e^3 : \varpi^3) &= 2,7774648 \\ l d\varphi &= -8,2227763 \\ l \sin s &= -9,9489752 \\ &+ 4,1994223 \end{aligned}$$

$$\begin{aligned} l \frac{r^2}{p} &= 3,2404707 \\ l \varpi &= 5,0032451 \\ l \cos \lambda &= 9,9985372 \\ l \sin s &= -9,9489752 \\ &- 8,1912282 \\ &+ 0,01553 \end{aligned}$$

$$\begin{aligned} \text{pars I} &= -2n \cdot 15828 \\ \text{pars II} &= +2n \cdot 49547 \\ dr &= +2n \cdot 33719 \\ dr &= +67438n \end{aligned}$$

$$\begin{aligned} \sin \mu &= 0,02965 \\ \dots &= 0,04518 \\ l \dots &= 8,6549462 \\ lu &= 5,0371515 \\ l \frac{r^2}{e} &= 0,0032451 \\ ld\varphi (\dots) &= -0,9996735 \\ &- 4,6950163 \end{aligned}$$

Pro variatione excentricitatis  $q$ :

$$\begin{aligned} ldp &= 4,8196097 \\ lqr &= 3,2278867 \\ &1,5917230 \\ &- 39,059n \\ &+ 38,764n \end{aligned}$$

$$\begin{aligned} lp &= 4,9874160 \\ ldr &= 4,8289047 \\ &9,8163207 \\ lqrr &= 8,2278867 \\ &1,5884340 \end{aligned}$$

$$2dq = -0,295n \text{ et } dq = -0,148n.$$

Pro variatione anguli  $\Omega LB = \alpha$ :

$$\begin{aligned} lp &= -4,9874160 \\ l\varpi &= 5,0032451 \\ l(1+q \cos s) &= 9,9841709 \\ l \cos \lambda &= 9,9985372 \\ l \cos s &= -9,6605005 \\ &- 9,6432086 \end{aligned}$$

$$\begin{aligned} 2+q \cos s &= 1,96421 \\ l(2+q \cos s) &= 0,2931857 \\ l \sin \mu &= 8,4720247 \\ l \sin s &= -9,9489752 \\ &- 8,7141856 \end{aligned}$$

pars postrema = - 0,43975 - 0,05178 = - 0,49153.

lars postrema = - 9,6915500  
 $l \frac{c^3}{u^3} = 2,7768972$   
 $l \frac{c^3}{u^3} = - 0,0497355$   
2,5181827

$l \frac{c^3}{u^3} = 2,7774648$   
 $l \cos \sigma = - 9,6605005$   
- 2,4379653  
 $l \text{agg} = 1,7451685$   
 $l \frac{c^3}{u^3} = 0,0097353$   
 $l - d\varphi = - 3,5372014$   
 $l \frac{1}{r} = 1,7721133$

lars posterior = + 329,748  
 lars prior = - 274,136  
 lars aggreg. = + 55,612

$d\alpha = - 11593600n \text{ min. sec.}$

- 7,0642185

variatione nodi et inclinationis:

$l^u = 0,0497355$   
 $l^p = 0,0097353$   
 $l \left( \frac{c^3}{u^3} - \frac{c^3}{u^3} \right) = 2,7768972$   
 $l d\varphi = - 3,5372014$   
 $l \sin \sigma = 9,4236974$   
 $l \sin (\vartheta - \psi) = 9,3941794$   
- 5,1914462

Ergo  $d\psi = + 155398n \text{ min. sec.}$   
 $l d\psi = 5,1914462$   
 $l \sin \omega = 9,4884240$   
4,6798702  
 $l \text{tang} \omega = 9,4395426$   
5,2403276  
 ergo  $d\omega = 173911n \text{ min. sec.}$

Calculus pro intervallo a 28 ad 29 Aprilis.

Hic erit  $\rho = 100775$ ;  $u = 110550$ ;  $\sigma = 14^\circ 25'$ ;  $s = - 118^\circ 12'$  et  $\vartheta - \psi = 15^\circ 14'$ , unde

pro  $d\varphi$  inventi

$l\varphi = 5,0033528$   
 $lu = 5,0435587$   
 $lp = 4,9874160$   
 $l^u = 0,0561427$   
 $l^p = 0,0097353$

$l d\sqrt{\varphi} = 13,5436916$   
 $l\omega = 10,0067056$   
 $l d\varphi = - 3,5369860$   
4,6855709  
 $l d\varphi = - 8,2225609$

nunc pro angulis  $\lambda$  et  $\mu$

$l \cos (\vartheta - \psi) = 9,9844660$   
 $l \cos \sigma = 9,9861045$   
 $l \sin \sigma = 9,3961499$   
9,9705705  
9,3806159  
+ 0,93448  
+ 0,06224  
 $\cos \lambda = 0,99672$   
 $\lambda = 4^\circ 38'$

$l \sin (\vartheta - \psi) = 9,4195436$   
 $l \cos \omega = 9,9783702$   
9,3979138  
 $l \sin \sigma = 9,3961499$   
 $l \cos \sigma = 9,9861045$   
8,7940637  
9,3840183  
+ 0,24022  
- 0,24211  
 $\sin \mu = - 0,00189$   
 $l \sin \mu = - 7,2764618$

unde colligitur distantia  $MN = \omega$  hoc modo

$$\begin{aligned} l\omega &= 5,0033528 \\ l \sin \lambda &= 8,9072975 \\ l \cos \lambda &= 9,9985784 \\ l\omega \sin \lambda &= 3,9106503 \\ l\omega \cos \lambda &= 5,0019312 \\ l \sin \nu &= 9,7974640 \\ l\omega &= 4,1131863 \\ l \frac{c}{w} &= 0,8868136 \\ l \frac{c^3}{w^3} &= 2,6604408 \\ \frac{c^3}{w^3} &= 457,55 \end{aligned}$$

Pro variatione parametri  $p$ :

$$\begin{aligned} l \frac{v^3}{c^3} &= 0,0100584 \\ lu &= 5,0435587 \\ l \sin \mu &= -7,2764618 \\ l \dots &= 2,6597356 \\ ld\varphi &= -9,2225609 \\ &+ 3,2123754 \end{aligned}$$

Pro variatione semiaxis transversae  $r$ :

$$\begin{aligned} l \frac{qrr}{p} &= 3,2404707 \\ l \frac{v^3}{c^3} &= 0,0100584 \\ l \frac{c^3}{w^3} &= 2,6604408 \\ ld\varphi &= -8,2225609 \\ l \sin s &= -9,9451255 \\ &+ 4,0786563 \\ \text{pars I} &= -2n \cdot 11985 \\ \text{pars II} &= +2n \cdot 11478 \\ dr &= -2n \cdot 507 \end{aligned}$$

seu

$$\begin{aligned} dr &= -1014n \\ ld\varphi &= -3,5134054 \\ lqr &= 3,2278867 \\ &- 0,2855187 \\ &+ 1,9298 \\ &- 0,5829 \end{aligned}$$

$$2 dq = +1,3469n \quad \text{et} \quad dq = +0,6735n.$$

$$\begin{aligned} u &= 110550 \\ \varphi \cos \lambda &= 100446 \\ \dots &= 10104 \\ l\omega \sin \lambda &= 3,9106503 \\ l \dots &= 4,0044933 \\ l \tan \nu &= 9,9061570 \\ \nu &= 38^\circ 51' \\ l \frac{c}{u} &= 9,9564413 \\ l \frac{c^3}{u^3} &= 9,8693239 \\ \frac{c^3}{u^3} &= 0,740 \\ \frac{c^3}{w^3} - \frac{c^3}{u^3} &= 456,81 \\ l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) &= 2,6597356 \end{aligned}$$

Ergo

$$\begin{aligned} dp &= -2n \cdot 1631 \\ \text{seu} \quad dp &= -3262n \\ ld\varphi &= -3,5134054 \end{aligned}$$

$$\begin{aligned} l \frac{q}{p} &= 3,2404707 \\ l \cos \lambda &= 5,0019312 \\ l \sin s &= -9,9451255 \\ &- 8,1875274 \\ \dots &+ 0,01540 \\ \sin \mu &= -0,00189 \\ \dots &0,01351 \\ l \dots &8,1306553 \\ lu &= 5,0435587 \\ l \frac{v}{c} &= 0,0033528 \\ ld\varphi &= -8,2225609 \\ l \left( \frac{c^3}{v^3} - \frac{c^3}{u^3} \right) &= 2,6597356 \\ &- 4,0598633 \\ lp &= 4,9874160 \\ ldr &= 3,0060380 \\ &- 7,9934540 \\ lqrr &= 8,2278867 \\ &- 9,7655673 \end{aligned}$$

Pro variatione anguli  $\Omega LB = \alpha$ :

$$\begin{aligned} l p &= 4,9874160 \\ l q &= 5,0033528 \\ l(1+q \cos s) &= 9,9840632 \\ l \cos \lambda &= 9,9985784 \\ l \cos s &= -9,6744485 \\ l p &= -9,6570901 \end{aligned}$$

$$\begin{aligned} 2+q \cos s &= 1,96397 \\ l(2+q \cos s) &= 0,2931349 \\ l \sin \mu &= -7,2764618 \\ l \sin s &= -9,9451255 \\ &= +7,5147222 \end{aligned}$$

pars postrema =  $-0,45404 + 0,00327 = -0,45077$

$$\begin{aligned} l \text{ partis postr.} &= -9,6539550 \\ l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) &= +2,6597356 \\ l \frac{u^2}{p} &= 0,0561427 \\ &= -2,3698333 \end{aligned}$$

$$\begin{aligned} l \frac{c^3}{w^3} &= 2,6604408 \\ l \cos s &= -9,6744485 \\ &= -2,3348893 \end{aligned}$$

pars post. =  $+234,33$

pars prior =  $-216,21$

aggreg. =  $+18,12$

$$\begin{aligned} l \text{ aggr.} &= 1,2581582 \\ l \frac{v^3}{c^3} &= 0,0100584 \\ l d\varphi &= -3,5369860 \\ l \frac{1}{q} &= 1,7721133 \\ &= -6,5773159. \end{aligned}$$

ergo  $d\alpha = -3778470 n \text{ min. sec.}$

Pro variatione nodi et inclinationis:

$$\begin{aligned} l \frac{u^2}{p} &= 0,0561427 \\ l \frac{v^3}{c^3} &= 0,0100584 \\ l \dots &= 2,6597356 \\ l d\varphi &= -3,5369860 \\ l \sin \sigma \sin (\vartheta - \psi) &= 8,8156935 \\ l - d\psi &= -5,0786162 \end{aligned}$$

Ergo  $d\psi = +119840 n \text{ min. sec.}$

$$\begin{aligned} l d\psi &= +5,0786162 \\ l \sin \omega &= 9,4884240 \\ l \cot \sigma &= 0,5899546 \\ &= +5,1569948 \end{aligned}$$

ergo  $d\omega = 143550 n \text{ min. sec.}$

Calculus pro intervallo a 29 ad 30 Aprilis.

Hic erit  $\varphi = 100800$ ;  $u = 112155$ ;  $\sigma = 13^\circ 23'$ ,  $s = -119^\circ 10'$  et  $\vartheta - \psi = 16^\circ 6'$ , unde pro  $d\varphi$  inventiend

$$\begin{aligned} l v &= 5,0034605 \\ l u &= 5,0498200 \\ l p &= 4,9874160 \\ l \frac{u^2}{p} &= 0,0624040 \end{aligned}$$

$$\begin{aligned} l c d \xi \sqrt{ep} &= 13,5436916 \\ l v &= 10,0069210 \\ l d\varphi &= -3,5367706 \\ &= 4,6855749 \\ l d\varphi &= -8,2223455 \end{aligned}$$

nunc pro angulis  $\lambda$  et  $\mu$ 

$$l \cos (\vartheta - \psi) = 9,9826236$$

$$l \cos \sigma = 9,9879223$$

$$l \sin \sigma = 9,3666036$$

$$9,9705459$$

$$9,3492272$$

$$+ 0,93443$$

$$+ 0,06137$$

$$\cos \lambda = 0,99580$$

$$\lambda = 5^{\circ} 15'$$

$$l \sin (\vartheta - \psi) = 9,4429728$$

$$l \cos \omega = 9,9783702$$

$$9,4213430$$

$$l \sin \sigma = 9,3666036$$

$$l \cos \sigma = 9,9879223$$

$$8,7879466$$

$$9,4092653$$

$$+ 0,22347$$

$$- 0,25660$$

$$\sin \mu = - 0,03313$$

$$l \sin \mu = - 8,5203525,$$

unde colligitur distantia  $MN = \omega$ 

$$l \omega = 5,0034605$$

$$l \sin \lambda = 8,9614288$$

$$l \cos \lambda = 9,9981743$$

$$l \nu \sin \lambda = 3,9648893$$

$$l \nu \cos \lambda = 5,0016348$$

$$l \sin \nu = 9,7899880$$

$$l \omega = 4,1749013$$

$$l \frac{c}{w} = 0,8250987$$

$$l \frac{c^3}{w^3} = 2,4752961$$

$$\frac{c^3}{w^3} = 298,74$$

$$\frac{c^3}{w^3} - \frac{c^3}{u^3} = 298,03$$

$$u = 112155$$

$$\nu \cos \lambda = 100377$$

$$\dots 11778$$

$$l \nu \sin \lambda = 3,9648893$$

$$l \dots 4,0710715$$

$$l \text{ tang } \nu = 9,8938178$$

$$\nu = 38^{\circ} 4'$$

$$l \frac{c}{u} = 9,9501800$$

$$l \frac{c^3}{u^3} = 9,8505400$$

$$\frac{c^3}{u^3} = 0,7088$$

$$l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = 2,4742600.$$

Pro variatione semiparametri  $p$ :

$$l \frac{\nu^3}{c^3} = 0,0103815$$

$$l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = 2,4742600$$

$$lu = 5,0498200$$

$$l \sin \mu = - 8,5203525$$

$$ld \varphi = - 8,2223455$$

$$+ 4,2771595$$

Ergo

$$dp = - 2n \cdot 18930$$

scu

$$dp = - 37860 n$$

et

$$ldp = - 4,5781895$$

per variationem semiaxis transversae r:

$$\begin{aligned} \frac{r}{p} &= 3,2404707 \\ \frac{r}{c} &= 0,0103815 \\ \frac{r}{w} &= 2,4752961 \\ \frac{r}{u} &= -8,2223455 \\ \frac{r}{s} &= -9,9411166 \\ &+ 3,8896104 \end{aligned}$$

$$\begin{aligned} \text{pars I} &= -2n.7756 \\ \text{pars II} &= -2n.10052 \\ \text{pars III} &= -2n.17808 \\ \text{pars IV} &= -35616n \end{aligned}$$

$$\begin{aligned} \frac{r}{p} &= 3,2404707 \\ l \cos \lambda &= 5,0016348 \\ l \sin s &= -9,9411166 \\ &= -8,1832221 \\ l \cos s &= -9,6878425 \\ \frac{r \cos \lambda \sin s}{p} &= +0,01525 \\ \sin \mu &= -0,03313 \\ \text{aggreg.} &= -0,01788 \\ l \text{ aggreg.} &= -8,2523675 \\ \frac{r}{c} &= 5,0532805 \\ l - d\varphi &= 8,2223455 \\ l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) &= 2,4742600 \\ &= -4,0022535. \end{aligned}$$

Quia datur  $q = V \left( 1 - \frac{p}{r} \right)$ , non opus est quaerere  $dq$ .

per variationem anguli  $\Omega LB = \alpha$ :

$$\begin{aligned} \frac{r}{p} &= 4,9874160 \\ \frac{r}{c} &= 5,0034605 \\ l \cos s &= 9,9839555 \\ \frac{r}{w} &= 9,9981743 \\ \frac{r}{u} &= -9,6878425 \\ &= -9,6699723 \end{aligned}$$

$$\begin{aligned} 2 + q \cos s &= 1,96373 \\ l(2 + q \cos s) &= 0,2930751 \\ l \sin \mu &= -8,5203525 \\ l \sin s &= -9,9411166 \\ &+ 8,7545442 \end{aligned}$$

$$\begin{aligned} \text{pars postrema} &= -0,46771 \\ &+ 0,05683 = -0,41088 \end{aligned}$$

$$\begin{aligned} \text{pars post.} &= -9,6137150 \\ \frac{r}{p} &= -0,0624040 \\ \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) &= 2,4742600 \\ &+ 2,1503790 \end{aligned}$$

$$\begin{aligned} \frac{r}{w} &= 2,4752961 \\ l \cos s &= -9,6878425 \\ &= -2,1631386 \\ l \text{ aggr.} &= -0,6242821 \\ \frac{r}{c} &= 0,0103815 \\ l d\varphi &= -3,5367706 \\ \frac{r}{q} &= 1,7721133 \\ &+ 5,9435475 \end{aligned}$$

$$\begin{aligned} \text{pars posterior} &= +141,38 \\ \text{pars prior} &= -145,59 \\ \text{aggreg.} &= -4,21 \end{aligned}$$

$$d\alpha = +878107n \text{ min. sec.}$$



Pro variatione nodi et inclinationis:

$$\begin{aligned} l \frac{u}{p} &= 0,0624040 \\ l \frac{v^3}{c^3} \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) &= 2,4846415 \\ l d\varphi &= -3,5367706 \\ l \sin \sigma \sin (\vartheta - \psi) &= 8,8095764 \\ &= -4,8933925 \end{aligned}$$

$$\begin{aligned} \text{ergo } d\psi &= +78234 n \text{ min. sec.} \\ l d\psi &= 4,8933925 \\ l \sin \omega &= 9,4884240 \\ l \cot \sigma &= 0,6213187 \\ l d\omega &= 5,0031352 \\ \text{ergo } d\omega &= +100724 n \text{ min. sec.} \end{aligned}$$

## Calculus pro intervallo a 30 Aprilis ad 1 Maji.

Hic erit  $v = 100825$ ;  $u = 113745$ ;  $\sigma = 12^\circ 29'$ ;  $s = -120^\circ 8'$  et  $\vartheta - \psi = 16^\circ 56'$ , unde  
pro  $d\varphi$  inveniend

$$\begin{aligned} l v &= 5,0035682 \\ l u &= 5,0559323 \\ l p &= 4,9874160 \\ l \frac{u}{p} &= 0,0685163 \end{aligned}$$

$$\begin{aligned} l d \zeta \sqrt{cp} &= 13,5436916 \\ l v \varphi &= 10,0071364 \\ l d\varphi &= -3,5365552 \\ &= 4,6855749 \\ l d\varphi &= -8,2221301. \end{aligned}$$

Nunc pro angulis  $\lambda$  et  $\mu$ 

$$\begin{aligned} l \cos (\vartheta - \psi) &= 9,9807505 \\ l \cos \sigma &= 9,9896095 \\ l \sin \sigma &= 9,3347665 \\ &= 9,9703600 \\ &= 9,3155170 \\ &= +0,93403 \\ &= +0,05990 \\ \cos \lambda &= +0,99393 \\ \lambda &= 6^\circ 38' \end{aligned}$$

$$\begin{aligned} l \sin (\vartheta - \psi) &= 9,4642790 \\ l \cos \omega &= 9,9783702 \\ &= 9,4426492 \\ l \sin \sigma &= 9,3347665 \\ l \cos \sigma &= 9,9896095 \\ &= 8,7774157 \\ &= 9,4322587 \\ &= +0,20678 \\ &= -0,27055 \\ \sin \mu &= -0,06377 \\ l \sin \mu &= -8,8046164, \end{aligned}$$

unde colligitur distantia  $MN = w$ 

$$\begin{aligned} l v &= 5,0035682 \\ l \cos \lambda &= 9,9973554 \\ l \sin \lambda &= 9,0414852 \\ l v \cos \lambda &= 5,0009236 \\ l v \sin \lambda &= 4,0450534 \\ l \sin \nu &= 9,8019735 \\ l w &= 4,2430799 \\ l \frac{c}{w} &= 0,7569201 \\ l \frac{c^3}{w^3} &= 2,2707603 \\ l \frac{c^3}{w^3} &= 186,536 \end{aligned}$$

$$\begin{aligned} u &= 113745 \\ v \cos \lambda &= 100213 \\ u - v \cos \lambda &= 13532 \\ l v \sin \lambda &= 4,0450534 \\ l (u - v \cos \lambda) &= 4,1313620 \\ l \tan \nu &= 9,9136914 \\ \nu &= 39^\circ 20' \\ l \frac{c}{u} &= 9,9440677 \\ l \frac{c^3}{u^3} &= 9,8322031 \\ \frac{c^3}{u^3} &= 0,680. \end{aligned}$$

$$\text{ergo } \frac{c^3}{w^3} - \frac{c^3}{u^3} = 185,856 \quad \text{et} \quad l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = 2,2691700.$$

ro variatione semiparametri  $p$ :

$$\begin{aligned}
 l \frac{v^3}{c^3} &= 0,0107046 \\
 l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) &= 2,2691700 \\
 lu &= 5,0559323 \\
 l \sin \mu &= -8,8046164 \\
 ld\varphi &= -8,2221301 \\
 &+ 4,3625534
 \end{aligned}$$

Ergo

$$\begin{aligned}
 dp &= -2n \cdot 23044 \\
 \text{seu } dp &= -46088n
 \end{aligned}$$

ro variatione semiaxis transversi  $r$ :

$$\begin{aligned}
 l \frac{qrr}{p} &= 3,2404707 \\
 l \frac{v^3}{c^3} &= 0,0107046 \\
 l \frac{c^3}{w^3} &= 2,2707603 \\
 ld\varphi &= -8,2221301 \\
 l \sin s &= -9,9369456 \\
 &+ 3,6810113
 \end{aligned}$$

$$\begin{aligned}
 l \frac{q}{p} &= 3,2404707 \\
 lv \cos \lambda &= 0,0009236 \\
 l \sin s &= -9,9369456 \\
 &+ 8,1783399 \\
 &+ 0,01508 \\
 \sin \mu &= -0,06377 \\
 \dots &= -0,04869
 \end{aligned}$$

$$\text{pars I} = -2n \cdot 4797,5$$

$$\text{pars II} = -2n \cdot 17308$$

$$dr = -2n \cdot 22105$$

$$dr = -44210n$$

$$\begin{aligned}
 l \dots &= -8,6874398 \\
 lu &= 5,0559323 \\
 l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) &= 2,2691700 \\
 ld\varphi &= -8,2221301 \\
 l \frac{v}{c} &= 0,0035682 \\
 &+ 4,2382404
 \end{aligned}$$

ro variatione anguli  $\Omega LB = \alpha$ :

$$\begin{aligned}
 lp &= 4,9874160 \\
 lv &= 5,0035682 \\
 l(1 + q \cos s) &= 9,9838478 \\
 l \cos \lambda &= 9,9973554 \\
 l \cos s &= -9,7007158 \\
 &+ 9,6819190
 \end{aligned}$$

$$\begin{aligned}
 2 + q \cos s &= 1,9635 \\
 l(2 + q \cos s) &= 0,2930309 \\
 l \sin \mu &= -8,8046164 \\
 l \sin s &= -9,9369456 \\
 &+ 9,0345929
 \end{aligned}$$

$$\begin{aligned}
 \text{pars postrema} &= -0,48075 \\
 &+ 0,10829 = -0,37246.
 \end{aligned}$$

$$l \text{ part. postr.} = -9,5710796$$

$$l \frac{u}{p} = 0,0685163$$

$$l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = 2,2691700$$

$$l \text{ part. post.} = -1,9087659$$

$$\text{pars posterior} = +81,052$$

$$\text{pars prior} = -89,676$$

$$\text{aggreg.} = -8,624$$

$$\begin{aligned}
 l \frac{c^3}{w^3} &= 2,2707603 \\
 l \cos s &= -9,6819190 \\
 l \text{ part. I} &= -1,9526793 \\
 l \text{ aggreg.} &= -0,9357087 \\
 l \frac{v^3}{c^3} &= 0,0107046 \\
 ld\varphi &= -3,5365552 \\
 l \frac{1}{q} &= 1,7721133 \\
 &+ 6,2550818
 \end{aligned}$$

$$d\alpha = +1799210n \text{ min. sec.}$$

Pro variatione nodi et inclinationis

$$\begin{aligned}
 l \frac{u}{p} &= 0,0685163 \\
 l p^3 \left( \frac{1}{w^3} - \frac{1}{u^3} \right) &= 2,2798746 \\
 l d\varphi &= -3,5365552 \\
 l \sin \sigma \sin (\vartheta - \psi) &= 8,7990455 \\
 l - d\psi &= -4,6839916
 \end{aligned}$$

Ergo

$$\begin{aligned}
 d\psi &= +48305 n \text{ min. sec.} \\
 l d\psi &= 4,6839916 \\
 l \sin \omega &= 9,4884240 \\
 l \cos \sigma &= 0,6548430 \\
 l d\omega &= 4,8272586 \\
 d\omega &= 67183 n \text{ min. sec.}
 \end{aligned}$$

Calculus pro intervallo a 1 ad 2 Maji.

Hic erit  $\varphi = 100850$ ;  $u = 115380$ ;  $\sigma = 11^\circ 31'$ ,  $s = -121^\circ 6'$ , et  $\vartheta - \psi = 17^\circ 45'$ , unde

pro  $d\varphi$  inveniendo

$$\begin{aligned}
 l v &= 5,0036759 \\
 l w &= 5,0621305 \\
 l p &= 4,9874160 \\
 l \frac{u}{p} &= 0,0747145
 \end{aligned}$$

$$\begin{aligned}
 l c d \zeta \sqrt{c p} &= 13,5436916 \\
 l v v &= 10,0073518 \\
 l d\varphi &= -3,5363398 \\
 &= 4,6855749 \\
 l d\varphi &= -8,2219147.
 \end{aligned}$$

Nunc pro angulis  $\lambda$  et  $\mu$

$$\begin{aligned}
 l \cos (\vartheta - \psi) &= 9,9788175 \\
 l \cos \sigma &= 9,9911670 \\
 l \sin \sigma &= 9,3002758 \\
 &= 9,9699845 \\
 &= 9,2790933
 \end{aligned}$$

$$\begin{aligned}
 l \sin (\vartheta - \psi) &= 9,4841066 \\
 l \cos \omega &= 9,9783702 \\
 &= 9,4624768 \\
 l \sin \sigma &= 9,3002758 \\
 l \cos \sigma &= 9,9911670 \\
 &= 8,7627526 \\
 &= 9,4536438
 \end{aligned}$$

$$\begin{aligned}
 &= +0,93322 \\
 &= +0,05791 \\
 \cos \lambda &= 0,99113 \\
 \lambda &= 7^\circ 38'
 \end{aligned}$$

$$\begin{aligned}
 &= +0,19015 \\
 &= -0,28421 \\
 \sin \mu &= -0,09406 \\
 l \sin \mu &= -8,9734050.
 \end{aligned}$$

unde colligitur distantia  $MN = \omega$ :

$$\begin{aligned}
 l v &= 5,0036759 \\
 l \cos \lambda &= 9,9961343 \\
 l \sin \lambda &= 9,1233061 \\
 l v \cos \lambda &= 4,9998102 \\
 l v \sin \lambda &= 4,1269820 \\
 l \sin \nu &= 9,8166521 \\
 l \omega &= 4,3103299 \\
 l \frac{c}{w} &= 0,6896701 \\
 l \frac{c^3}{w^3} &= 2,0690103 \\
 \frac{c^3}{w^3} &= 117,22 \\
 \frac{c^3}{w^3} - \frac{c^3}{u^3} &= 116,75
 \end{aligned}$$

$$\begin{aligned}
 u &= 115380 \\
 v \cos \lambda &= 99956 \\
 u - v \cos \lambda &= 15424 \\
 l v \sin \lambda &= 4,1269820 \\
 l (u - v \cos \lambda) &= 4,1881970 \\
 l \tan \nu &= 9,9387850 \\
 \nu &= 40^\circ 58' \\
 l \frac{c}{u} &= 9,9378695 \\
 l \frac{c^3}{u^3} &= 9,8136085 \\
 \frac{c^3}{u^3} &= 0,65 \\
 l \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) &= 2,0665868.
 \end{aligned}$$

et

Pro variatione semiparametri  $p$ :

$$\begin{aligned}
 l_{c^2}^{o^2} &= 0,0110277 \\
 l_{\dots} &= 2,0665868 \\
 lu &= 5,0621305 \\
 l \sin \mu &= -8,9734050 \\
 ld\varphi &= -8,2219147 \\
 &+ 4,3350647
 \end{aligned}$$

Ergo

$$\begin{aligned}
 dp &= -2n \cdot 21630 \\
 \text{seu } dp &= -43260n
 \end{aligned}$$

Pro variatione semiaxis  $r$ :

$$\begin{aligned}
 l_{p}^{qrr} &= 3,2404707 \\
 l_{c^2}^{o^2} &= 0,0110277 \\
 l_{w^2}^{c^2} &= 2,0690103 \\
 ld\varphi &= -8,2219147 \\
 l \sin s &= -9,9326092 \\
 &+ 3,4750326
 \end{aligned}$$

$$\begin{aligned}
 l_{p}^q &= 3,2404707 \\
 l \cos \lambda &= 4,9998102 \\
 l \sin s &= -9,9326092 \\
 &- 8,1728901 \\
 &+ 0,01489 \\
 \sin \mu &= -0,09406 \\
 &- 0,07917
 \end{aligned}$$

$$\begin{aligned}
 \text{pars I} &= -2n \cdot 2985,6 \\
 \text{pars II} &= -2n \cdot 17900 \\
 dr &= -2n \cdot 20886 \\
 dr &= -41772n
 \end{aligned}$$

$$\begin{aligned}
 l_{\dots} &= -8,8985606 \\
 l_{c}^{uv} &= 5,0658064 \\
 ld\varphi &= -8,2219147 \\
 l_{\dots} &= 2,0665868 \\
 &+ 4,2528685
 \end{aligned}$$

Pro variatione anguli  $\Omega$   $LB = \alpha$ :

$$\begin{aligned}
 lp &= 4,9874160 \\
 lv &= 5,0036759 \\
 l(1 + q \cos s) &= 9,9837401 \\
 l \cos \lambda &= 9,9961343 \\
 l \cos s &= -9,7130983 \\
 &- 9,6929727
 \end{aligned}$$

$$\begin{aligned}
 2 + q \cos s &= 1,9633 \\
 l(2 + q \cos s) &= 0,2929867 \\
 l \sin \mu &= -8,9734050 \\
 l \sin s &= -9,9326092 \\
 &+ 9,1990009
 \end{aligned}$$

$$\begin{aligned}
 \text{pars postrema} &= -0,49314 \\
 &+ 0,15812 = -0,33502.
 \end{aligned}$$

$$\begin{aligned}
 l_{\text{part. post.}} &= -9,5250707 \\
 l_{\dots} &= 2,0665868 \\
 l_{p}^u &= 0,0747145 \\
 &- 1,6662720
 \end{aligned}$$

$$\begin{aligned}
 l_{w^2}^{c^2} &= 2,0690103 \\
 l \cos s &= -9,7130983 \\
 &- 1,7821086 \\
 l_{\text{aggreg.}} &= -1,1515537 \\
 l_{c^2}^{o^2} &= 0,0110277 \\
 ld\varphi &= -3,5365398 \\
 l_{q}^1 &= 1,7721133 \\
 &+ 6,4712345
 \end{aligned}$$

$$\begin{aligned}
 \text{pars posterior} &= +46,373 \\
 \text{pars prior} &= -60,549 \\
 \text{aggreg.} &= -14,176
 \end{aligned}$$

Ergo  $d\alpha = +2959610n$  min. sec.

Pro variatione nodi et inclinationis:

$$l \frac{u}{p} \left( \frac{c^3}{w^3} - \frac{c^3}{u^3} \right) = 2,1413013$$

$$l \frac{v^3}{c^3} = 0,0110277$$

$$ld\varphi = 3,5365398$$

$$l \sin \sigma \sin (\vartheta - \psi) = 8,7843824$$

$$-4,4732512$$

ergo

$$d\psi = +29734 n \text{ min. sec.}$$

$$ld\psi = 4,4732512$$

$$l \sin \omega = 9,4889240$$

$$l \cot \sigma = 0,6908912$$

$$4,6525664$$

ergo

$$d\omega = 44933 n \text{ min. sec.}$$

### Conclusio.

Cum variationes inventae sint admodum notabiles, simili modo tam ante terminum 25 Aprilis quam post 2 Maj. definiri debent. Quas igitur computavi hic simul aspectui exponam:

Intervallum Aprilis	$dp$	$dr$	$da$	$d\psi$	$d\omega$
15 - 16					
16 - 17					
17 - 18					
18 - 19					
19 - 20					
20 - 21	+ 45310n	+ 144570n	- 4937360n	+ 8903n	+ 6717n
21 - 22					
22 - 23					
23 - 24					
24 - 25					
25 - 26	+ 155650n	+ 154346n	- 19059570n	+ 112880n	+ 111364n
26 - 27	+ 135314n	+ 135466n	- 18445310n	+ 152436n	+ 159996n
27 - 28	+ 66010n	+ 67438n	- 11593600n	+ 155398n	+ 173911n
28 - 29	- 3262n	- 1014n	- 3778470n	+ 119840n	+ 143550n
29 - 30	- 37860n	- 35516n	+ 878107n	+ 78234n	+ 100724n
30 - 1 Maj.	- 46088n	- 44210n	+ 1799210n	+ 48305n	+ 67183n
1 - 2	- 43260n	- 41772n	+ 2959610n	+ 29734n	+ 44933n
2 - 3					
3 - 4					
4 - 5					
5 - 6					
6 - 7	- 19031n	- 17736n	+ 1554230n	+ 3608n	+ 9506n

Si certiores essemus de elementis motus hujus cometae, operae pretium esset hunc calculum ulterius tam in antecedentia quam consequentia extendere; nunc autem sufficiat conjectura tantum perturbationes in motu terrae ortas crassa minerva colligere.

## De variatione parametri.

Semiparameter  $p$  usque ad 28 Aprilis augetur, tum vero iterum minuitur; verumtamen augmenta multum praevalent. Videtur autem totum augmentum exurgere ad  $700000 n$ , unde cum ante cometæ adventum fuerit semiparameter  $p = 97144$ , is deinceps erit  $= 97144 + 700000 n$ . Quare si massa cometæ aequalis esset massae terrae, ob  $n = \frac{1}{200000}$ , fieret is  $= 97144 + 3\frac{1}{2}$ ; si massa cometæ ad massam terrae rationem  $= m:1$  habere ponatur, in postremum erit semiparameter  $= 97144 + \frac{7m}{2}$ .

## De variatione axis transversi.

Semiaxis transversus  $r$ , qui ante cometæ adventum sumtus est  $= 100000$ , fere similes mutationes patitur, quae autem aliquantillum erunt minores, ita ut augmentum totum aestimari queat quasi  $= 690000 n$ , et semiaxis post discessum cometæ  $= 100000 + 690000 n$ . Hinc posita ratione massae cometæ ad massam terrae  $= m:1$ , erit semiaxis in posterum  $= 100000 + \frac{69m}{20}$ .

## De variatione excentricitatis.

Cum sit in genere excentricitas  $q = \sqrt{1 - \frac{p}{r}}$ , eaque ante cometæ adventum fuerit  $= 0,0169$ , erit ea deinceps  $= \sqrt{1 - \frac{97144 - 3,5m}{100000 + 3,45m}} = \sqrt{0,01856 - 0,0000015m}$ , ideoque fiet excentricitas  $= 0,0169 - 0,000044m$

hoc est aliquanto minor quam ante. Quare si massa cometæ centies superaret massam terrae, ut esset  $m = 100$ , foret excentricitas  $= 0,0125$ , maximaque solis aequatio multo minor esset futura.

## De variatione anni solaris.

Ob auctum axem transversum quantitas anni solaris augebitur in ratione

$$1 : \left(1 + \frac{69m}{2000000}\right)^{\frac{3}{2}} = 1 : 1 + \frac{207m}{4000000}$$

Cum igitur ante adventum cometæ annus fuerit  $365^d 5^h 49'$ , annus in posterum augmentum capiet  $= 27m$  min. primorum. Dum ergo cometa esset terrae aequalis, annus 27 min. primis produceretur, fieretque  $= 365^d 6^h 16'$ . Ac si cometa adeo centies terram superaret, anni quantitas augmentum caperet 45 horarum, qui effectus sane foret stupendus.

## De variatione lineae absidum.

Usque ad diem 29 Aprilis linea absidum maxime promovetur, tum vero iterum repellitur; sed promotio plurimum praevalet atque ad minimum  $100000000 n$  aestimanda videtur. Hinc si ut hactenus massa cometæ  $m$  vicibus major ponatur, quam massa terrae, ab actione cometæ linea absidum orbitae terrae per spatium  $500 m$  min. sec. promovebitur. Ergo si cometa terrae esset aequalis, haec promotio esset  $= 8' 20''$ , sin autem centies esset major, foret ea  $13^{\circ} 23' 20''$ .

*De variatione lineae nodorum et inclinationis.*

Linea nodorum seu intersectio  $L\Omega$  ab actione cometæ super ejus orbita ad minimumum promovebitur per spatium  $950000 n$  min. sec. et inclinatio fere tantundem augebitur: unde utraque perturbatio erit  $47\frac{1}{2}m$  min. sec., quæ eo minus est dubia, cum actio cometæ perpetuo augmen-

Fig. 191. Consideremus hæc elementa in coelo, sitque  $\Omega C$  via cometæ,  $\Omega \cap \varepsilon$  ecliptica, adventum cometæ, erit angulus  $\cap \Omega C = 17^\circ 56' = \Omega$ , et arcus  $\Omega \cap = 51^\circ 16'$ , per  $\cap$  transibit æquator  $\mathcal{A} \cap Q$  faciens cum ecliptica angulum  $\mathcal{A} \cap \varepsilon = 23^\circ 28\frac{1}{2}'$ . Post effectum cometæ sit circulus  $\varepsilon o \lambda$  ecliptica secans priorem in  $o$ , erit  $\Omega \omega = d\psi$  et  $C\omega o = \Omega + d\omega$ . Ductur arculus  $\omega u$  ad  $\Omega o$  normalis, erit  $\Omega u = d\psi \cos \Omega$  et  $\omega u = d\psi \sin \Omega$ ; ponatur  $\Omega o = z$ , erit  $\sin z : \sin(z - d\psi \cos \Omega) = \sin(\Omega + d\omega) : \sin \Omega$ , unde fit  $\text{tang } z = \frac{d\psi \sin \Omega}{d\omega}$ , ergo  $d\omega = d\psi$ , erit  $l \text{ tang } z = l \sin \Omega = 9,4884240$ , ac propterea  $z = \Omega o = 17^\circ 7'$ ; tum vero  $o \sin z = d\psi \sin \Omega$  erit  $o = \frac{d\psi \sin \Omega}{\sin z} = 1,0512d\psi = 50m$  min. sec.; ob  $d\psi = d\omega = 47\frac{1}{2}m$ . Cum ergo sit  $\cap o = -34^\circ 9'$ , ecliptica quasi gyratur circa punctum  $m 4^\circ 9'$  per angulum  $50m$  min. sec. ut punctum solstitiale  $\varepsilon$  magis ab æquatore removeatur et obliquitas eclipticæ augeatur. Ductur  $\cap \mu$  ad  $o\omega$  normali, erit  $\cap \mu = -50m \sin 34^\circ 9'$ ,

$$\text{hincque} \quad \cap \lambda = \frac{-50m \cdot \sin 34^\circ 9'}{\sin 23^\circ 28\frac{1}{2}'}, \quad \text{et} \quad \mu \lambda = \frac{-50m \cdot \sin 34^\circ 9'}{\text{tang } 23^\circ 28\frac{1}{2}'}$$

Unde si obliquitas eclipticæ pristina vocetur  $= \varepsilon$  et nova  $= \varepsilon + d\varepsilon$ , erit

$$\sin \varepsilon : \sin(\varepsilon + d\varepsilon) = \sin(-34^\circ 9' - \mu \lambda) : \sin -34^\circ 9' \quad \text{seu} \quad d\varepsilon = 50m \cos 34^\circ 9' = 41m \text{ sec.}$$

et cum sit  $\mu \lambda = -63m$  sec. puncta æquinoctialia super ecliptica per  $63m$  sec. promota erunt, senda, super æquatore autem per spatium  $70m$  sec. In latitudine igitur stellarum, quarum longitudo est  $\Omega 4^\circ 9'$ , iste effectus maximè spectabitur, dum stellarum borealium latitudo minuetur, australium vero augebitur particula  $50m$  sec. In stellis vero sub longitudine  $\approx 4^\circ 9'$  sitis contrarium eveniet.

Si massa cometæ multum superet massam terræ, hæc perturbationes ad enormem quantitatem exurgere poterunt, ita ut effectum non solum in Astronomia, sed etiam in vita communi sensuri. Quin etiam, cum de elementis orbitæ cometæ non simus satis certi, error in eam incidere posset, ut omnes hæc perturbationes multo adeo majores essent prodituri, quam hic invenimus. Omnino autem etiamsi ob errores has perturbationes minui oporteret, et massa cometæ minor esset quam terræ, tamen ab hoc tempore novam quasi epocham constitui conveniet, pro qua novæ tabulæ solares ante omnia essent condendæ, quod negotium nonnisi pluribus elapsis annis perfici poterit. Lunares autem tabulæ multo majorem ac difficiliorem emendationem requisituræ videntur.