

Principles of Calculus Modeling: An Interactive Approach by Donald Kreider, Dwight Lahr, and Susan Diesel  
Exercises for Section 2.14

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1. (1 pt)

Find the linearization of the function  $3x^2 + 3x$  at the point where  $x = -1$ .

$$L(x) = \underline{\hspace{2cm}}$$

2. (1 pt)

Find the linearization of the function  $\sqrt{-4 - x}$  at the point where  $x = -5$ .

$$L(x) = \underline{\hspace{2cm}}$$

3. (1 pt)

Find the linearization of the function  $\cos(x)$  at the point where  $x = -0.25\pi$ .

$$L(x) = \underline{\hspace{2cm}}$$

4. (1 pt)

Find the linearization of the function  $\cos^2(x)$  at the point where  $x = \frac{7}{6}\pi$ .

$$L(x) = \underline{\hspace{2cm}}$$

5. (1 pt)

Use a suitable linearization to approximate  $\sqrt{83}$ .

Linear approximation of  $\sqrt{x}$ :

$$L(x) = \underline{\hspace{2cm}}$$

$$\sqrt{83} \approx \underline{\hspace{2cm}}$$

6. (1 pt)

Use a suitable linearization to approximate  $\sqrt[4]{259}$ .

Linear approximation of  $\sqrt[4]{x}$ :

$$L(x) = \underline{\hspace{2cm}}$$

$$\sqrt[4]{259} \approx \underline{\hspace{2cm}}$$

7. (1 pt)

Use a suitable linearization to approximate  $\cos\left(\frac{13}{60}\pi\right)$ .

Linear approximation of  $\cos(x)$ :

$$L(x) = \underline{\hspace{2cm}}$$

$$\cos\left(\frac{13}{60}\pi\right) \approx \underline{\hspace{2cm}}$$

8. (1 pt)

In this problem you will compare two methods of estimating a square root. When you use linear approximation to approximate  $\sqrt{65}$ , you consider the equation  $f(x) = \sqrt{x}$  and work with the tangent line to the graph of  $y = f(x)$  at  $(64, 8)$ . If you use Newton's Method, you consider  $g(x) = x^2 - 65$  and look for a root of this equation.

Find a linear approximation to  $f(x)$ , starting at  $(64, 8)$  to get an approximation for  $\sqrt{65}$ .

$$\sqrt{65} \approx \underline{\hspace{2cm}}$$

Perform one iteration of Newton's Method for  $g(x)$  starting at  $x_0 = 8$ .

$$\sqrt{65} \approx \underline{\hspace{2cm}}$$

9. (1 pt)

Find the linearization of the function  $-2x^3 + 10\sin x$  at the point where  $x = \pi$ .

$$L(x) = \underline{\hspace{2cm}}$$

10. (1 pt)

Find the linearization of the function  $f(x) = e^x$  at the point where  $x = 5$ .

$$L(x) = \underline{\hspace{2cm}}$$