

# Math 2

## Homework 1

Due: January 11, 2010

1. Calculate

$$\lim_{x \rightarrow 1} \frac{\sin(x)}{x - 1}$$

or show that the limit does not exist.

2. Using the limit definition of the derivative, calculate  $f'(x)$ , where

$$f(x) = 3x^2 + 2x + 1 + e^x.$$

You may use the fact that  $\lim_{h \rightarrow 0} \frac{e^h - 1}{h} = 1$ .

3. Find  $f'(x)$ , where  $f(x) = \sin(e^{x^2})$ .

4. Let  $f(x) = 3x^2 + 2x + 1$ ,  $g(x) = \sin(x)e^x$  and  $h(x) = f(g(x))$ . Find  $h'(x)$ .

5. Sketch the graph of  $f(x) = \cos^2(x)$  on the interval  $[-\pi, 2\pi]$ .

6. Sketch the graph of  $f(x) = 3 + \ln(2x)$  on the interval  $(0, 5]$ . Label any absolute maxima/minima.

7. Sketch the graph of  $f(x) = e^{-x}$  on the interval  $(-\infty, \infty)$ . Label any absolute maxima/minima.

8. Sketch the graph of

$$y = \frac{x}{\sqrt{1 - x^2}}.$$