We are familiar with the prime numbers as those integers which cannot be factored into smaller integers, but if we consider systems of numbers larger than the integers, the primes may indeed factor in those larger systems. We discuss various questions mathematicians ask how the primes may react in larger number systems. We will talk about both classical results and current research on the topic, and give a sense of the kind of tools needed to tackle these questions.