

## Errata

This list of errata is maintained by the author. Contributions are welcome. If you notice additional instances that are incorrect, misleading, or poorly explained, please notify the author at [dana@math.dartmouth.edu](mailto:dana@math.dartmouth.edu).

This page was last updated on November 12, 2023 at 10:21.

- Page 11, lines 21 & 22:** “ $\beta_V$ ” should be “ $\eta_V$ ”.
- Page 12, line 10:** Replace “ $U = r^{-1}(U)$ ” by “ $U = r^{-1}(U) \cap V$ ”.
- Page 16, line 6:** Replace “completion and” by “completion”.
- Page 17, line 2:** Replace “ $\gamma^{-1}$ ” with “ $\gamma^{-1}$ ”.
- Page 17, line –3:** Replace “ $|f(\gamma\eta^{-1})|$ ” with “ $|f(\gamma\eta^{-1})|$ ”.
- Page 19, line 7:** Replace “,” with “,”.
- Page 19, line –6:** “ $(\|\varphi\|_\infty \cdot 1 - |\varphi|^2)$ ” should be “ $(\|\varphi\|_\infty^2 \cdot 1 - |\varphi|^2)$ ”.
- Page 19, line –3:** “ $\|\varphi\|^2$ ” should be “ $\|\varphi\|_\infty^2$ ”.
- Page 20 line 16:** Replace “that is hard” with “that it is hard”.
- Page 29, Definition 2.1:** Replace “a map” with “a surjection”.
- Page 33, Definition 2.19:** Replace “if and” with “if”.
- Page 35, Corollary 2.26:** The hypothesis that  $G$  act freely was omitted.
- Page 37, Ex 2.1.10:**  $G$  must have an open range map for the implication that  $\pi(G)$  closed implies  $G \setminus G^{(0)}$  is Hausdorff.
- Page 37, Ex 2.1.18:** The result is correct but the proof needs to altered. See below for page 360.
- Page 45, line –10:** Replace “continuous open map” with “continuous open surjection”.
- Page 47, line 14:** Replace “ $w = y \cdot \eta$ ” with “ $z = y \cdot \eta$ ”.
- Page 47, line –13:** “ $w = h \cdot \beta$ ” should be “ $w = y \cdot \beta$ ”.
- Page 48, Corollary 2.50:** Replace “If the range map on  $H$  is open” with “If the range maps on  $H$  and  $G$  are both open”.
- Page 49, line 13:** Replace “continuous map” with “continuous surjection”.
- Page 57, line –7:** The displayed equation should be

$$\sigma_Z^u(\varphi) = \int_H \varphi(z \cdot \eta) d\beta^{s(z)}(\eta) \quad \text{for } \varphi \in C_c(Z).$$

- Page 58-9, Theorem 2.69:** Replace “ $\kappa|_{G^{(0)}}$ ” and “ $\kappa|_{G^{(0)}}$ ” by “ $\kappa|_G$ ” and “ $\kappa|_H$ ”, respectively. Here if  $u \in G^{(0)}$ , then  $(\kappa|_G)^u$  is meant to be the restriction of  $\kappa^u$  to the open subset  $G^u$  of  $L^u$ .
- Page 60, Theorems 2.70 and 2.71:** Replace “(2.7), and (2.8)” by “(2.8), and (2.9)”.
- Page 75, Proposition 3.14:** In part (a), replace “ $\dot{\beta}(\varphi)$ ” with “ $\dot{\beta}(\varphi)(G \cdot x)$ ”.
- Page 75, Proposition 3.16:** In part (b), replace “ $s : Z \rightarrow G^{(0)}$ ” by “ $s : Z \rightarrow H^{(0)}$ ”.

- Page 80, line 1:** “ $\mu_i \ll \mu$ ” should be “ $\mu_i \ll \mu_0$ ”.
- Page 81, line –13:** “ $p(H)$ ” should be “ $p_0(H)$ ”. This error is repeated multiple times.
- Page 81, line –19:** “ $G^{(0)} \times H \times G$ ” should be “ $G^{(0)} \times \Sigma_0 \times G$ ”.
- Page 82, lines 11, 15, and –14:** “ $p(H)$ ” should be “ $p_0(H)$ ”.
- Page 99, Theorem 4.9:** Replace “ $\|F\|_{C_r^*(G)} = \|f\|_{C_r^*(G)}$ ” with “ $\|F\|_{C^*(G)} = \|f\|_{C^*(G)}$ ”.
- Page 113, Ex 5.2.2:** The assertion is correct, but the “solution” contains a flaw. See the errata for page 372.
- Page 120, Line –15:** Replace “ $V(f)$ ” by “ $L(f)$ ”.
- Page 114, line 15:** Replace “ $\gamma_i \rightarrow s(\gamma)$ ” by “ $\gamma_i \rightarrow \gamma$ ”.
- Page 115, Eq (5.9):** Replace “ $\lambda^{r(z)}$ ” by “ $\lambda^{r(\zeta)}$ ”.
- Page 116, Eq (5.13):** Replace “ $I_k$ ” by “ $J_k$ ”.
- Page 178, line 14:** Replace the sentence “Since  $\nu$  is regular, we may as well assume that  $A$  is a  $G_\delta$ -set.” With “Since  $\nu$  is regular,  $\nu(A)$  is null if and only if every compact subset of  $A$  is null. Since  $\gamma \mapsto \gamma^{-1}$  is a homeomorphism, we can assume that  $A$  is a compact null set.” (See also the comments to Lemma 8.22 on page 180 below.)
- Page 178, line 19:** Replace “monotone convergence theorem” with “Dominated Convergence Theorem”.
- Page 180, Proof of Lemma 8.22:** The proof must be adjusted since the characteristic function  $\mathbb{1}_M$  of a precompact Borel set is in  $\mathcal{B}_c^1(G)$  if and only if  $M$  is both a  $G_\delta$ -set and a  $F_\sigma$ -set. A similar restriction applies to  $\mathbb{1}_N$  and  $\mathcal{B}_c^1(G^{(0)})$ . However, since  $\nu$  and  $L_{a,b}$  are both Radon measures, regularity allows us to assume that  $M$  is compact. Then  $f = \mathbb{1}_M \in \mathcal{B}_c^1(G)$  as claimed. Note that Equation (8.18) holds with  $\mathbb{1}_N$  replaced by  $\mathbb{1}_U$  for any  $U \supset N$ . Since  $N$  we can assume  $N$  is  $G_\delta$ , there are precompact open sets  $U_n$  such that  $U_{n+1} \subset U_n$  and  $N = \bigcap_n U_n$ . Since  $\mathbb{1}_{U_n} \in \mathcal{B}_c^1(G^{(0)})$ , we have
- $$L_{[g \otimes h, d \otimes k]}(f) = (M(\mathbb{1}_{U_n})L_b(f)[g \otimes h] \mid [d \otimes k]) \quad \text{for all } n \geq 1.$$
- But it is not hard to see that the Dominated Convergence Theorem implies that  $M(\mathbb{1}_{U_n}) \rightarrow M(\mathbb{1}_N)$  in the weak operator topology. This allows us to conclude that
- $$L_{[g \otimes h, d \otimes k]}(f) = (M(\mathbb{1}_N)L_b(f)[g \otimes h] \mid [d \otimes k]).$$
- Now the proof concludes as before.
- Page 189, Definition 9.3(b):** “ $x \mapsto f_i * f_i^*(\gamma)$ ” should be “ $\gamma \mapsto f_i * f_i^*(\gamma)$ ”.
- Page 190, item (b)’:** “ $x \mapsto g_i * g_i^*(\gamma)$ ” should be “ $\gamma \mapsto g_i * g_i^*(\gamma)$ ”.
- Page 190, Lemma 9.5:** For consistency, the variable  $x$  should be replaced with  $\gamma$ .
- Page 298, Definition 11.18:** It should have been remarked that if  $G$  is discretely trivial at  $v$ , then  $G(v)$  itself is trivial; that is,  $G(v) = \{v\}$ . This is implied by the definition by letting  $K$  be any nonempty compact subset of  $G(v) \setminus \{v\}$ .
- Page 301, line –11:** Replace “maps” with “map”.
- Page 309, line –2:** Replace “ker  $R$ ” with “ker  $\underline{R}$ ”.
- Page 303, lines 3, 6, and –1:** Replace “ $R$ ” with “ $\underline{R}$ ”.
- Page 360, Ex 2.1.18:** The proof of (c) $\implies$ (a) assumes the action is free. This is not necessary. Replace the last sentence with the following: “Since

$(y, x) \in R(G, X)$ ,  $y = \gamma \cdot x$  for some  $\gamma \in G$ . Since the source map is open, we can pass to a subnet, relabel, and assume that there are  $\eta_i \rightarrow \gamma^{-1}$  with  $s(\eta_i) = r(\gamma_i)$ . Then  $\eta_i \gamma_i \cdot x_i \rightarrow x$ . Since the  $X$  is Cartan, we can pass to a subnet and assume  $\eta_i \gamma_i \rightarrow \eta$ . But then  $\gamma_i \rightarrow \gamma \eta$ .

**Page 363, line 7 of Ex 2.3.8:** Replace “converging to  $s(z)$ ” with “converging to  $w$ ”.

**Page 372, Ex 5.2.2:** Replace the first sentence of the “solution” by “If  $U \cap F \neq \emptyset$ , there is a  $\varphi \in C_c(G^{(0)})$  such that  $\varphi$  vanishes off  $U$  and is not identically zero on  $F$ .”