Generalized Filtrations of Banach and Fredholm Manifolds

Abstract: We extend the deformation to the normal cone and tangent groupoid constructions from finite-dimensional manifolds to infinite-dimensional Banach and Fredholm manifolds. Next, we generalize the concept of Fredholm filtrations to get a more flexible and functorial theory. In particular, we show that if M is a Banach (or Fredholm) manifold with generalized filtration $\mathcal{F} = \{M_n\}_1^{\infty}$ by finite-dimensional submanifolds, then there are induced generalized filtrations $T\mathcal{F} = \{TM_n\}_1^{\infty}$ of the tangent bundle TM and $\mathbb{T}\mathcal{F} = \{\mathbb{T}M_n\}_1^{\infty}$ of the tangent groupoid $\mathbb{T}M$, which is not possible in the classical theory. The is joint work with Ahmad Reza.