

Mathematics 111  
Spring 2007  
Homework 6

1. Find all rational and Jordan canonical forms of a matrix in  $M_5(\mathbb{C})$  having minimal polynomial  $x^2(x-1)$ . Be sure to give the corresponding invariants and the characteristic polynomial.
2. Show that any linear operator  $T$  on a finite dimensional vector space (over a field of characteristic not equal to 2) which satisfies  $T^2 = I$  is diagonalizable. Give all possible Jordan forms for  $4 \times 4$  matrices.