Dartmouth College

Mathematics 115 — Practice Problems 2

1. Let $V = M_2(\mathbb{Q})$ viewed as a quadratic space of dimension 4 with associated quadratic form $q(A) = \det A$. Determine the Witt decomposition of (V, q), characterize its bilinear form in a natural way, and give an orthogonal basis for the space.