Reading Assignment # 8

Math 13 - Prof. Orellana

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Read Sections 3.2, 3.3 and 3.4

Don't forget to let me know the pages where you found the answers.

- 1. What does it mean for a path to be "nonrectifiable"? Give an example of such a path.
- 2. Define a vector field and explain how one would sketch a vector field in \mathbb{R}^2 or \mathbb{R}^3 . Give an example and sketch it.
- 3. What is the inverse square vector field in \mathbb{R}^3 ? Tell me what its direction is and its magnitude.
- 4. Define a gradient field and a potential function. What does the remark in page 210 says?
- 5. What is an equipotential set?
- 6. Define a flow line and sketch the vector field in Exercise 1 and indicate a flow line.
- 7. Define divergence and read the last paragraph in page 215 and tell me how I can intuitively think about the divergence.
- 8. When you take the divergence of a vector field, what do you get?
- 9. What does "incompressible" vector field means? Give an example of an incompressible vector field (you can use theorem 4.4 to construct one) and one that is not.
- 10. Define the curl of a vector field. Read the last paragraph of page 217 and explain what curl measures.
- 11. What does it mean for a vector field to be irrotational? Give an example of an irrotational vector field (you can use Theorem 4.3 to construct one) and one that is not irrotatitional.
- 12. What does Theorem 4.3 say? What does Theorem 4.4 say?