

H.W. 3  
Due Monday Jan. 26th

Tuesday:  $u$ -substitution with limits of integration

Use  $u$ -substitution as given in the problem to transform the definite integral shown. Then use the limits of integration determined by  $u$  to evaluate the integral.

(i)

$$\int_0^2 x e^{x^2} dx$$
$$u = x^2$$

(ii)

$$\int_{-2}^{-1} 2x \cos(x^2) \sin^2(x^2) dx$$
$$u = \sin(x^2)$$

Wednesday and Friday: Integration by Parts (Reverse Product Rule)

Use integration by parts (possibly multiple times) and/or  $u$ -substitution, where appropriate, to evaluate the following integrals:

\*You need only do one of (v), (vi) and (vii)\*

(i)

$$\int_0^{-1} x^2 \cos(x^3) dx$$

(ii)

$$\int_0^{\pi/4} \cos(3x) \sin(4x) dx$$

(iii)

$$\int_0^2 (6x^2 + 2x)(2x^3 + x^2)^{-3/4} dx$$

(iv)

$$\int_0^{\pi/4} \cos(x)\sin(x) dx$$

\*(v)

$$\int_0^1 x^7 e^{x^4} dx$$

\*(vi)

$$\int_{\sqrt{\frac{\pi}{2}}}^{\sqrt{\pi}} \frac{1}{x^5} \sin\left(\frac{1}{x^2}\right) dx$$

\*(vii)

$$\int_0^{\ln(\pi/4)} e^{3x} \sin(e^x) dx$$