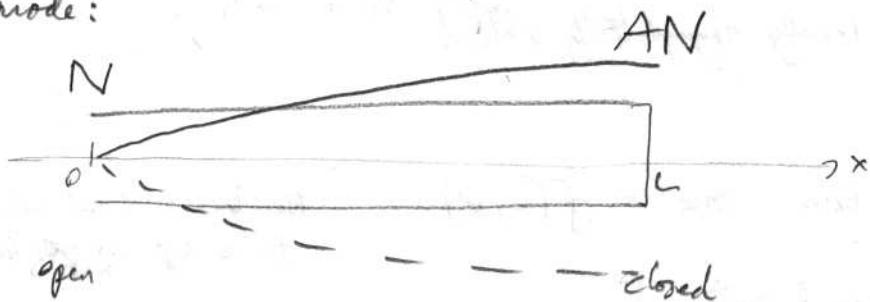


MATH 5 WORKSHEET : Pipe mode frequencies

Barrett
5/4/07

If one end open, other closed ('open-closed' pipe), get
(pressure) { Node at open end
{ Anti Node at closed end.

1st mode:

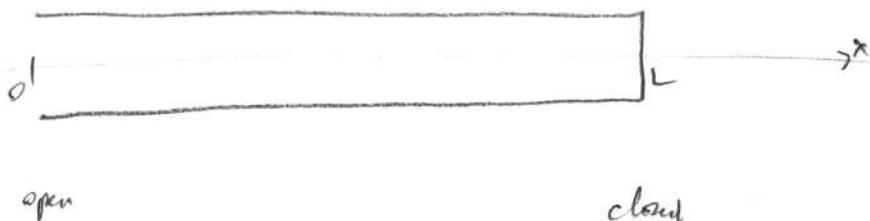


I've drawn mode shape.
What fraction of a wavelength λ is L ?

So what is frequency f_1 ?
(in terms of L, c)

2nd mode:

{ draw the next mode that matches the boundary conditions,
labelling N, AN locations.



What fraction of λ is L ?

So what is the freq.?

What is general rule for frequencies (mode n)?

Which harmonics of fundamental are present?

MATH 5 WORKSHEET : Pipe mode frequencies

Barnett
5/4/07

If one end open, other closed ('open-closed' pipe), get

(pressure) $\begin{cases} \text{Node at open end} \\ \text{Anti Node at closed end.} \end{cases}$

1st mode:



$\lambda/2$

I've drawn mode shape.
What fraction of a wavelength λ is L ?

open —————— closed

$$L = \lambda/4$$

$\lambda/4$

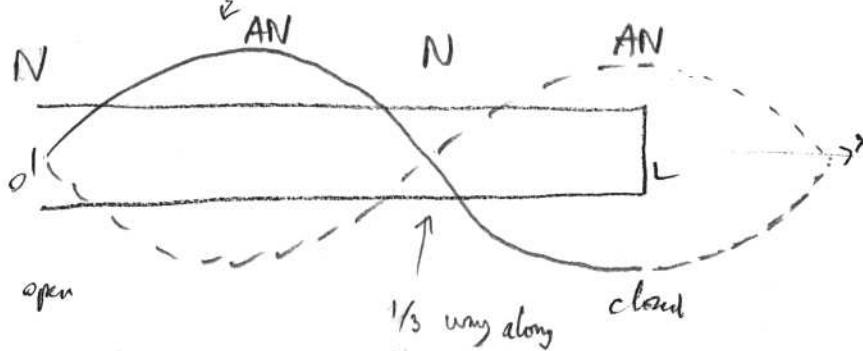
So what is frequency f_1 ?

(in terms of L, c)

$$f_1 = \frac{c}{\lambda} = \frac{c}{4L}$$

2nd mode:

draw the next mode that matches the boundary conditions,
labelling N, AN locations.



1/3 way along
from closed end
(it's where to
put a register key in a clarinet)

What fraction of λ is L ?

$$3/4, \text{ ie } \lambda = \frac{4}{3}L$$

So what is the freq.? $f_2 = \frac{c}{\lambda/3} = 3 \frac{c}{4L}$

What is general rule for frequencies (mode n)?

$$f_n = (2n-1) \frac{c}{4L}$$

Which harmonics of fundamental are present? 1, 3, 5, ... just odd.