

### Homework 3: Due Wednesday, April 23

**Section 4.1:** #6, 22, 24, 34, 46, 52, 54

**Section 4.2:** #2, 8

**Problem:** Suppose that you are playing poker with a friend. Each of you is dealt five cards at random from one deck (so you can not both have the same card). You happen to get dealt a flush, and you want to know whether your friend is more or less likely to have a flush based on this information. Thus, we let  $E$  be the event “You have a flush” and let  $F$  be the event “Your friend has a flush”. Calculate  $P(F|E)$ . How does this value compare to  $P(F)$ ? Are  $E$  and  $F$  independent events?

**Problem:** The game of Spades consists of 2 team with 2 players each. In one round, the 52 cards are dealt so that each player gets 13 cards. Let  $X$  be the random variable which gives the number of spades that you have. Let  $Y$  be the random variable which gives the number of spades that your partner has. Calculate  $P(X = 2, Y = 4)$  (this is one value of the joint distribution of  $X$  and  $Y$ ). Are  $X$  and  $Y$  independent random variables?