

## Math 71 Homework

### Due Monday, October 31st.

- Page 116: Problems 2 and 3 (from section 4.1).
  - And work the following problem:
1. (a) Show that there is a well-defined homomorphism  $\phi : \mathbf{Z}/18\mathbf{Z} \rightarrow \mathbf{Z}/12\mathbf{Z}$  which sends  $\bar{1}$  to  $\bar{10}$ . (More explicitly,  $\phi$  maps the class of 1 in  $\mathbf{Z}/18\mathbf{Z}$  to the class of 10 in  $\mathbf{Z}/12\mathbf{Z}$ .)
    - (b) Show that there is no such map sending  $\bar{1}$  to  $\bar{3}$ .
    - (c) Compute the kernel of  $\phi$ .
    - (d) Identify  $\text{Im } \phi$  with a well-known group using the Third Isomorphism Theorem.