

Worksheet #19

(1) Evaluate the limit.

$$\lim_{t \rightarrow 2} \left( \frac{t^2 - 2t}{t - 2} \mathbf{i} + \sqrt{t + 4} \mathbf{j} + \frac{\sin(\pi t)}{\ln(t - 1)} \mathbf{k} \right)$$

(2) Sketch the curve  $\mathbf{r}(t) = \langle t^2, \sqrt{t}, 1 \rangle$ . Use arrows to indicate the direction in which  $t$  increases.

(3) Find the unit tangent vector  $\mathbf{T}(t)$  of  $\mathbf{r}(t) = \langle \cos(t), -\sin(t), \sin(2t) \rangle$  when  $t = \pi/2$ .

(4) Evaluate the integral.

$$\int_0^{\pi/2} (3 \sin^2 t \cos t \mathbf{i} + 2 \sin t \cos^2 t \mathbf{j} + 2 \sin t \cos t \mathbf{k}) dt$$