

Worksheet #6

(1) Use the monotonic convergence theorem to prove the sequences converge.

(a) $a_n = \frac{4n-3}{2^n}$

(b) $a_{n+1} = 1 + \frac{1}{2}a_n$ where $a_1 = 1$. (This is a recurrence relation. See page 723 for an example.)

(2) Determine whether each integral is convergent or divergent. Evaluate those that are convergent.

(a) $\int_2^3 \frac{1}{\sqrt{3-x}} dx$

(b) $\int_{-\infty}^{\infty} \cos(\pi t) dt$

(c) $\int_1^{\infty} \frac{\ln x}{x} dx$

(d) $\int_4^{\infty} \frac{1}{\sqrt{x-3}} dx$