## Math 8

Winter 2020
Preliminary Homework
Assigned Wednesday, January 29
Note: Preliminary homework is always graded credit or no credit. You get full credit for completing the assignment, whether or not your answers are correct, as long as your work shows you have thought about the problem. The purpose of preliminary homework is to start you thinking about the topic of the next class.

You may use your preliminary homework for in-class activities with your classmates. You should be sure to think about these questions so you will be prepared.

Preliminary homework is always due at the beginning of the next class.

(1.) Suppose the vector in $\mathbb{R}^{2}$ from $(0,0)$ to $\left(x_{1}, y_{1}\right)$ has length $r_{1}$ and makes an angle of $\alpha$ with the $x$-axis, where $0<\alpha<\frac{\pi}{2}$. Express the sine and cosine of $\alpha$ in terms of $x_{1}, y_{1}$, and $r_{1}$.

Hint: Use the right triangle with corners $(0,0)\left(x_{1}, 0\right),\left(x_{1}, y_{1}\right)$.
(2.) Suppose the vector in $\mathbb{R}^{2}$ from $(0,0)$ to $\left(x_{2}, y_{2}\right)$ has length $r_{2}$ and makes an angle of $\beta$ with the $x$-axis, where $\alpha<\beta<\frac{\pi}{2}$. Express the sine and cosine of $\beta$ in terms of $x_{2}, y_{2}$, and $r_{2}$.
(3.) Let $\theta$ be the angle between the vector from $(0,0)$ to $\left(x_{1}, y_{1}\right)$ and the vector from $(0,0)$ to $\left(x_{2}, y_{2}\right)$. Express the cosine of $\theta$ in terms of $x_{1}, x_{2}, y_{1}, y_{2}, r_{1}$, and $r_{2}$.

Hint: Notice that $\theta=\beta+(-\alpha)$ and use the trigonometric identity

$$
\cos \left(\theta_{1}+\theta_{2}\right)=\cos \left(\theta_{1}\right) \cos \left(\theta_{2}\right)-\sin \left(\theta_{1}\right) \sin \left(\theta_{2}\right)
$$

